

**1973-2009 INDEX of PROBLEMS & SOLUTIONS**  
for  
**THE COLLEGE MATHEMATICS JOURNAL**  
**(Including the TWO YEAR COLLEGE MATHEMATICS JOURNAL)**

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Notes:

1. All entries are in the format:

**Problem Number.**

**Proposer, Volume .Issue Number(Year)Page** of publication

**Topic of problem** as interpreted by the indexer

**Solution Title** determined by the Problem Editors **Volume .Issue Number(Year)Page**

2. The Two Year College Mathematics Journal began publishing in 1970, but the problem section did not begin until Volume 4 in 1973.
3. Please report any errors or omissions to the indexer at <charliecook29150@aim.com>.
4. \*\*\*\*\* indicates problems for which a solution is pending.

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893.  
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894.  
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