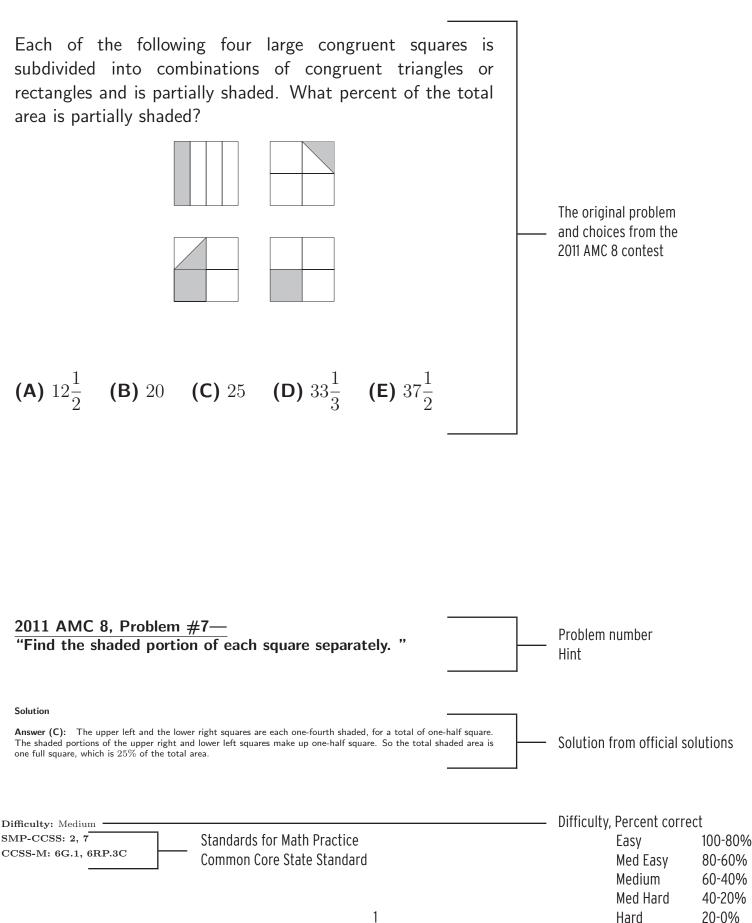
# AMC 10/12 Student Practice Questions

Guide to Student Practice Questions



What is  $10 \cdot (\frac{1}{2} + \frac{1}{5} + \frac{1}{10})^{-1}$ ?

(A) 3 (B) 8 (C) 
$$\frac{25}{2}$$
 (D)  $\frac{170}{3}$  (E) 170

2014 AMC 10A, Problem #1—

### "Sum up the fractions before working on multiplication"

Solution

Answer (C): Note that

$$10 \cdot (\frac{1}{2} + \frac{1}{5} + \frac{1}{10})^{-1} = 10 \cdot (\frac{5}{10} + \frac{2}{10} + \frac{1}{10})^{-1}$$
$$= 10 \cdot (\frac{8}{10})^{-1}$$
$$= \frac{25}{2}.$$

Difficulty: Medium Easy

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them, 2. Reason Abstractly and Quantitatively **CCSS-M:** 8.EE.A. Work with radicals and integer exponents.

On an algebra quiz, 10% of the students scored 70 points, 35% scored 80 points, 30% scored 90 points, and the rest scored 100 points. What is the difference between the mean and the median of the students' scores on this quiz?

## (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

#### 2014 AMC 10A, Problem #5—

"What is the median score if 50% of the students scored 90 or lower, and over 50% of the students scored 90 or higher?"

#### Solution

Answer (C): Because over 50% of the students scored 90 or lower, and over 50% of the students scored 90 or higher, the median score is 90. The mean score is

 $\frac{10}{100} \cdot 70 + \frac{35}{100} \cdot 80 + \frac{30}{100} \cdot 90 + \frac{25}{100} \cdot 100 = 87,$ 

for a difference of 90 - 87 = 3.

 $\mathbf{Difficulty:} \ \mathrm{Medium}$ 

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them, 2. Reason Abstractly and Quantitatively. **CCSS-M:** S-1D.B. Summarize, represent, and interpret data on two categorical and quantitative variables.

#### AMC 10/12 Student Practice Questions continued

Which of the following numbers is a perfect square?

(A) 
$$\frac{14!15!}{2}$$
 (B)  $\frac{15!16!}{2}$  (C)  $\frac{16!17!}{2}$  (D)  $\frac{17!18!}{2}$  (E)  $\frac{18!19!}{2}$ 

#### 2014 AMC 10A, Problem #8-

#### "What is the fraction for a perfect square?"

Solution

Answer (D): Note that  $\frac{n!(n+1)!}{2} = (n!)^2 \cdot \frac{n+1}{2}$ , which is a perfect square if and only if  $\frac{n+1}{2}$  is a perfect square. Only choice D satisfies this condition.

Difficulty: Hard

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them. **CCSS-M:** 

The two legs of a right triangle, which are altitudes, have lengths  $2\sqrt{3}$  and 6. How long is the third altitude of the triangle?

(A) 1 (B) 2 (C) 3 (D) 4 (E) 5

#### 2014 AMC 10A, Problem #9—

"What is the area of the triangle and the hypotenuse length ny the Pythagorean Theorem?"

Solution

Answer (C): The area of the triangle is  $\frac{1}{2} \cdot 2\sqrt{3} \cdot 6 = 6\sqrt{3}$ . By the Pythagorean Theorem, the hypotenuse has length  $4\sqrt{3}$ . The desired altitude has length  $\frac{6\sqrt{3}}{\frac{1}{2} \cdot 4\sqrt{3}} = 3$ .

 $\mathbf{Difficulty:}\ \mathrm{Medium}\ \mathrm{Hard}$ 

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them, 7. Look For and Make Use of Structure. **CCSS-M:** G-SRT. Understand similarity in terms of similarity transformations.

David drives from his home to the airport to catch a flight. He drives 35 miles in the first hour, but realizes that he will be 1 hour late if he continues at this speed. He increases his speed by 15 miles per hour for the rest of the way to the airport and arrives 30 minutes early. How many miles is the airport from his home?

(A) 140 (B) 175 (C) 210 (D) 245 (E) 280

#### 2014 AMC 10A, Problem #15—

# "What is the remaining distance after one hour of driving, and the remaining time until his flight?"

#### Solution

Answer (C): Let d be the remaining distance after one hour of driving, and let t be the remaining time until his flight. Then d = 35(t+1), and d = 50(t-0.5). Solving gives t = 4 and d = 175. The total distance from home to the airport is 175 + 35 = 210 miles.

OR

Let d be the distance between David's home and the airport. The time required to drive the entire distance at 35 MPH is  $\frac{d}{35}$  hours. The time required to drive at 35 MPH for the first 35 miles and 50 MPH for the remaining d-35 miles is  $1 + \frac{d-35}{50}$ . The second trip is 1.5 hours quicker than the first, so

$$\frac{d}{35} - \left(1 + \frac{d - 35}{50}\right) = 1.5.$$

Solving yields d = 210 miles.

Difficulty: Medium Hard

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them, 2. Reason Abstractly and Quantitatively. **CCSS-M:** A-CED. Create equations that describe numbers or relationships.

Susie pays for 4 muffins and 3 bananas. Calvin spends twice as much paying for 2 muffins and 16 bananas. A muffin is how many times as expensive as a banana?

(A) 
$$\frac{3}{2}$$
 (B)  $\frac{5}{3}$  (C)  $\frac{7}{4}$  (D) 2 (E)  $\frac{13}{4}$ 

#### 2014 AMC 10B, Problem #4-

## "What is the cost of muffin and a banana?"

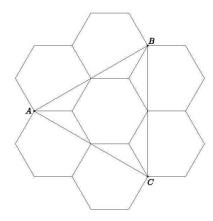
Solution

Answer (B): Let a muffin cost m dollars and a banana cost b dollars. Then 2(4m + 3b) = 2m + 16b, and simplifying gives  $m = \frac{5}{3}b$ .

Difficulty: Medium Easy

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them, 2. Reason Abstractly and Quantitatively. **CCSS-M:** A.SSE.B. Write expressions in equivalent forms to solve problems.

Six regular hexagons surround a regular hexagon of side length 1 as shown. What is the area of  $\triangle ABC$ ?



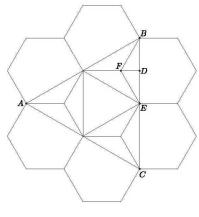
(A)  $2\sqrt{3}$  (B)  $3\sqrt{3}$  (C)  $1 + 3\sqrt{2}$  (D)  $2 + 2\sqrt{3}$  (E)  $3 + 2\sqrt{3}$ 

#### 2014 AMC 10B, Problem #13—

"What is the midpoint of  $\overline{BE}$ ?"

Solution

**Answer (B):** Label points E and F as shown in the figure, and let D be the midpoint of  $\overline{BE}$ . Because  $\triangle BFD$  is a  $30-60-90^{\circ}$  triangle with hypotenuse 1, the length of  $\overline{BD}$  is  $\frac{\sqrt{3}}{2}$ , and therefore  $BC = 2\sqrt{3}$ . It follows that the area of  $\triangle ABC$  is  $\frac{\sqrt{3}}{4} \cdot (2\sqrt{3})^2 = 3\sqrt{3}$ .



OR

Notice that AE = 3 since AE is composed of a hexagon side (length 1) and the longest diagonal of a hexagon (length 2). Triangle ABE is  $30-60-90^{\circ}$ , so  $BE = \frac{3}{\sqrt{3}} = \sqrt{3}$ . The area of  $\triangle ABC$  is  $AE \cdot BE = 3\sqrt{3}$ .

Difficulty: Medium

**SMP-CCSS:** 1. Make Sense of Problems and Persevere in Solving Them. **CCSS-M:** G.SRT. Similarity, Right Triangles, and Trigonometry.