where A_0, \ldots, A_{m_1-1} are arbitrary constants and the functions ϕ_1 , $\{C_k\}_{k=0}^{m_1-1}$ and f_{m_1} are defined by the formulas

$$\phi_1(x) = \int_c^x \frac{b_1(t)}{a_1(t)} dt, C_0(x) = 1, f_{m_1}(x) = \frac{1}{(m_1 - 1)!} \int_c^x (x - t)^{m_1 - 1} \frac{f(t)}{a_1(t)} dt$$

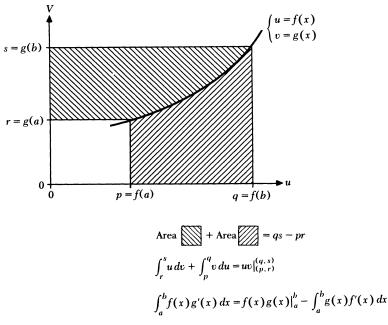
and for $k \ge 1$,

$$C_k(x) = \frac{1}{(k-1)!} \int_c^x \frac{(x-t)^{k-1}}{a_1(t)} dt.$$

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Proof without Words: Integration by Parts



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