

**1970-2022.3 TOPIC INDEX**  
for  
*The College Mathematics Journal*  
(including the *Two Year College Mathematics Journal*)

prepared by  
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Each item in this index is listed under the topics for which it might be used in the classroom or for enrichment after the topic has been presented. Within each topic entries are listed in chronological order of publication. Each entry is given in the form:

**Title, author, volume:issue, year, page range, [C or F], [other topic cross-listings]**

where C indicates a classroom capsule or short note and F indicates a Fallacies, Flaws and Flimflam note. If there is nothing in this position the entry refers to an article unless it is a book review.

The topic headings in this index are numbered and grouped as follows:

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- 4 Linear Algebra
  - 4.1 Matrices, systems of linear equations, and matrix algebra
  - 4.2 Determinants (also see 5.5)
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  - 4.4 Linear transformations
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  - 4.7 Other topics in linear algebra
  - 4.8 Software for linear algebra
- 5 Calculus
  - 5.1 Limits and differentiation
    - 5.1.1 Limits (including l'Hopital's rule)
    - 5.1.2 The derivative and mean value theorems
    - 5.1.3 Tangents, differentials, and differentiation
    - 5.1.4 Maxima and minima
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  - 5.2 Integration
    - 5.2.1 Definition of integrals and the fundamental theorem
    - 5.2.2 Numerical integration
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    - 5.2.4 Partial fraction decomposition
    - 5.2.5 Integration by parts
    - 5.2.6 Area
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    - 5.2.10 Improper integrals
  - 5.3 Elementary and special functions
    - 5.3.1 Inverse trigonometric functions
    - 5.3.2 Exponential and logarithmic functions
    - 5.3.3 Hyperbolic functions and their inverses
    - 5.3.4 Special functions
  - 5.4 Sequences and series
    - 5.4.1 Sequences
  - 5.4.2 Numerical series (convergence tests and summation)
  - 5.4.3 Taylor polynomials and power series
- 5.5 Vector algebra and geometry (and 3x3 determinants)
- 5.6 Curves and surfaces
  - 5.6.1 Parametric and polar curves
  - 5.6.2 Surfaces and coordinate systems in space

- 5.7 Multivariable calculus
    - 5.7.1 Multivariable differential calculus
    - 5.7.2 Multiple integrals
    - 5.7.3 Line and surface integrals and vector analysis
  - 5.8 Software for calculus
- 6 Differential Equations and Dynamical Systems
- 6.1 First order equations
  - 6.2 Higher order linear equations and linear systems
  - 6.3 Difference equations, dynamical systems, and fractals
  - 6.4 Nonlinear differential equations
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- 7 Probability and Statistics
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- 9 Other Topics
- 9.1 Set theory and logic (also see 0.9)
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### 0 Precalculus Mathematics (also see 9)

#### 0.1 Arithmetic (also see 9.3)

- Remedial or Developmental? Confusion over Terms, Don Ross, 1:2, 1970, 27-31, 1.2  
Two-Pan Weighings, Chris Burditt, 3:2, 1972, 80-81, C  
Cyclically Permuted Code: A Variation on Binary Arithmetic, J. Maurice Kingston, 5:1, 1974, 29-36  
Computation of Repeating Decimals, James E. McKenna, 7:2, 1976, 55-58  
Smith Numbers, A. Wilansky, 13:1, 1982, 21, 9.3  
Cryptology: From Ceasar Ciphers to Public-Key Cryptosystems, Dennis Luciano and Gordon Prichett, 18:1, 1987, 2-17, 7.2, 9.3  
What's Significant about a Digit?, David A. Smith, 20:2, 1989, 136-139, C, 9.6  
FFF #85. Unto Everyone That Hath Shall Be Given, John W. Kenelly, 26:1, 1995, 36, F  
Number Words in English, Steven Schwartzman, 26:3, 1995, 191-195  
The Mathematical Judge: A Fable, William G. Frederick and James R. Hersberger, 26:5, 1995, 377-381, 1.1  
The Square of Any Odd Number is the Difference Between Two Triangular Numbers (Proof Without Words), Roger B. Nelsen, 27:2, 1996, 118, C, 9.3  
Fractions with Cycling Digit Patterns, Dan Kalman, 27:2, 1996, 109-115, 9.3  
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A large square consisting only of digits 7, 8 and 9, Hisanori Mishima, 34:4, 2003, 303, C, 9.3  
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Federal Money, Joseph Crukshank, 36:3, 2005, 208, C

FFF #242. Lighter than air, Marie S. Wilcox, 36:4, 2005, 316-317, F

Wrong, Wrong, and Wrong: Math Guides Are Recalled, *New York Times*, 36:5, 2005, 362, C

Where are the missing “8-terms”? Johann Hoehn and Larry Hoehn, 37:1, 2006, 68, C

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Three Poems, Caleb Emmons, 40:3, 2009, 188, 9.2

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Teaching Tip: Accepting that  $.999\dots = 1$ , David W. Cohen and James M. Henle, 40:4, 2009, 258, C

Brown Sharpie:  $.999\dots = 1$  (Cartoon), Courtney Gibbars, 40:4, 2009, 262, C

Fallacies, Flaws and FlimFlam: What’s *Your* Version of Two-Thirds?, Mary Ann Bragg, 40:5, 2009, 343, C

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A Pumping Lemma for Invalid Reductions of Fractions, Michael N. Fried and Mayer Goldberg, 41:5, 2010, 357-364, 9.3

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Flaws, Fallacies, and Flimflam: Who’s Right?, Fred Graf, Megan McArdle, and Ed Barbeau, 42:1, 2011, 55, C

Flaws, Fallicies, and Flimflam: What Day Is It?, Allen Schwenk, 42:3, 2011, 205, F (see also 5. The International Dateline, 42:5, 2011, 430-431)

Minuend & Subtrahend, Merriam-Webster Dictionary, 42:4, 2011, 316, C

Student Research Project: Making Change Efficiently, Jack E. Graver, 42:4, 2011, 317-322, 3.2, 5.1.4, 9.9

Just Take the Limit!, Jody Picoult, 42:5, 2011, 431, C, 0.8, 9.10

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Carryless Arithmetic Mod 10, David Applegate, Marc LeBrun, and N. J. A. Sloane, 43:1, 2012, 43-50, 5.4.1, 9.2, 9.4

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- Proof Without Words: Triangular Sums, Yuko Kobayashi, 44:3, 2013, 189, C, 9.3  
 Zbikowski's Divisibility Criterion, Yonah Cherniavsky and Artour Mouftakhov, 45:1, 2014, 17-21, 9.3  
 Proof Without Words: Limit of a Recursive Arithmetic Mean, Angel Plaza, 45:5, 2014, 364, C, 5.1.1,  
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 Groupoid Cardinality and Egyptian Fractions, Julia E. Bergner and Christopher D. Walker, 46:2, 2015,  
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 Partial Proof Without Words: Shaping Some Cases of the Erdos-Straus Conjecture, 46:3, 2015, 181, C,  
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 Square-Sum Pair Partitions, Gordon Hamilton, Kiran S. Kedlaya, and Henri Picciotto, 46:4, 2015, 264-  
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 Proof Without Words: A Surprising Integer Result, Roger B. Nelsen, 47:2, 2016, 94, C, 0.3  
 Multiplying by 9, Arthur Benjamin and Rohan Chandra, 47:4, 2016, 281, C, 0.2  
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 Factoring Numbers with Conway's 150 Method, Arthur T. Benjamin, 49:2, 2018, 122-125, 9.3  
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 Converting Between Dates in the Hebrew and Roman Calendars, John Conway , Gabrielle Agus & David  
     Slusky , 51:5, 2020, 322-329, 9.2  
 An Infinite Family of Divisibility Tests, Darrin Frey and Adam Hammett, 52:1, 2021, 2-10, 9.3

## 0.2       Algebra

- Mathematics, A Solitary Game, Olof Hanner, 1:2, 1970, 5-16, 4.1  
 Gog and Gug, Howard W. Eves, 1:1, 1970, 8, C  
 The Irrationality of Certain Numbers, Peter A. Lindstrom, 1:1, 1970, 30-31, 9.3  
 A Computer-Oriented Multiplication Algorithm, John Peterson, 1:2, 1970, 106, C  
 A Geometric Approach to the Orders of Infinity, Harold L. Schoen, 3:2, 1972, 74-76, C, 9.5  
 Pascal's k-Simplex, Dale Woods and Mary Jane Kohlenberg, 4:3, 1973, 38-43  
 Teaching Inequalities Involving Absolute Values, Frances W. Lewis, 4:2, 1973, 87-90, C  
 Maximize  $x(a-x)$ , L. H. Lange, 5:1, 1974, 22-24, 0.7, 5.1.4  
 A Geometric Approach to Linear Programming in the Two-Year College, Pat Semmes, 5:1, 1974, 37-40,  
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 A Further Note on the Orders of Infinity, Harold L. Schoen, 5:1, 1974, 80-81, C, 9.5  
 Investigations of Linear and Reciprocal Functions by the Line-to-Line Technique, David R. Duncan and  
     Bonnie H. Litwiller, 6:2, 1975, 2-7, 0.7  
 Distributivity with Respect to All Four Rational Operations, Myles Greene, 6:2, 1975, 10-12  
 Mathematical Induction: If Student k Understands It, Will Student K + 1?, Judith L. Gersting, 6:2, 1975,  
     18-20, 0.9  
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 Mathematics and Computing without Computers, William S. Dorn, 8:2, 1977, 101-105  
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- Stirling's Numbers of the Second Kind—Programming Pascal's and Stirling's Triangles, Satish K. Janardan and Konanur G. Janardan, 9:4, 1978, 243-248, 6.3
- Some Pre-Calculus Algebra, John Staib, 10:2, 1979, 89-95
- The Discovery of a Generalization: An Example in Problem Solving, Hugh Ouellette and Gordon Bennett, 10:2, 1979, 100-106, 0.3
- Polygonal Roots, Barnabas B. Hughes, 10:5, 1979, 313-318, 0.7
- Distance from a Point to a Line, Warren B. Gordon, 10:5, 1979, 348-349, C
- A Technique for Determining When a General Quadratic Expression is Factorable, Leo Chosid, 10:5, 1979, 354-355, C, 0.7
- Luddhar's Method of Solving a Cubic Equation with a Rational Root, R. S. Luthar, 11:2, 1980, 107-110, 0.7
- Computer Solution of Alphametics, Sarah Brooks, 11:2, 1980, 111-114
- Why Not Teach Synthetic Multiplication?, Kenneth R. Kundert, 11:2, 1980, 121-122, C
- A Precalculus Approximation of  $n!$ , Norman Schaumberger, 11:3, 1980, 202-204, C, 5.4.2
- An Error-Detecting Check by Substitution, Charles G. Moore, 11:5, 1980, 326-327, C
- A "Proof" that  $M=N$ , W. Thurmon Whitley, 12:3, 1981, 211, C
- Inventor's Paradox, Man-Keung Siu, 12:4, 1981, 267, C
- Misguided Mathematical Maxim-Makers, Betsy Darken Smith, 12:5, 1981, 309-316, 1.2
- A Classroom Approach to Pythagorean Triples, Norman Schaumberger, 13:1, 1982, 61-62, C
- Selection of a Fair Currency Exchange Rate, Allen J. Schwenk, 13:2, 1982, 154-155, C, 0.8
- An Alternate Method for Solving Radical Equations, Bill Bompert, 13:3, 1982, 198-199, C
- The Thrills of Abstraction, P. R. Halmos, 13:4, 1982, 243, 1.2
- Isomorphisms on Magic Squares, Ali R. Amir-Moez, 14:1, 1983, 48-51, 5.4.1, 9.2, 9.3, 9.4
- A Logarithm Algorithm for Four-Function Calculators, David Cusick, 14:4, 1983, 322, 5.3.2
- The Address Problem, Michael Tennen, 14:5, 1983, 407-414, 9.3
- Approximation of Square Roots, Leon Wejntrub, 14:5, 1983, 427-430, 0.7, 9.6
- Antisubmarine Warfare: Passive vs. Active Sonar, L. Whitt and K. Wilk, 14:5, 1983, 434-435, C
- Is the Venn Diagram Good Enough?, Mou-Liang Kung and George C. Harrison, 15:1, 1984, 48-50, 9.1
- A Geometrical Interpretation of the Weighted Mean, Larry Hoehn, 15:2, 1984, 135-139, 0.4, 7.3
- On Problems with Solutions Attainable in More Than One Way, Jean Pedersen and George Polya, 15:3, 1984, 218-228, 0.4, 5.4.2
- Complex Roots Made Visible, Alec Norton and Benjamin Lotto, 15:3, 1984, 248-249, C, 0.7
- Pythagorean Systems of Numbers, Joseph Wiener, 15:4, 1984, 324-326, C, 0.4, 9.3
- An Approach to Problem-Solving Using Equivalence Classes Modulo n, James E. Schultz and William F. Burger, 15:5, 1984, 401-405, 9.3
- The Factorial Triangle and Polynomial Sequences, Steven Schwartzman, 15:5, 1984, 424-426, C, 5.4.1, 6.3
- Right Triangles with Perimeter and Area Equal, William Parsons, 15:5, 1984, 429, C, 0.4
- What Do I Know? A Study of Mathematical Self-Awareness, Philip J. Davis, 16:1, 1985, 22-41, 9.3
- Nested Polynomials and Efficient Exponential Algorithms for Calculators, Dan Kalman and Warren Page, 16:1, 1985, 57-60, C, 0.7, 9.6
- Behold! The Arithmetic-Geometric Mean Inequality, Roland H. Eddy, 16:3, 1985, 208, C, 0.3
- Instances of Simpson's Paradox, Thomas R. Knapp, 16:3, 1985, 209-211, C, 7.3
- Approximating Solutions for Exponential Equations, Norman Schaumberger, 16:3, 1985, 211-212, C
- Graphing the Complex Roots of a Quadratic Equation, Floyd Vest, 16:4, 1985, 257-261, C, 0.7, 9.5
- A New Divisibility Algorithm, Joseph Whittaker, 16:4, 1985, 268-276, 9.3
- A Discrete Look at  $1 + 2 + \dots + n$ , Loren C. Larson, 16:5, 1985, 369-382, 0.9, 3.1, 3.2, 5.4.2, 6.3
- Routine Problems, Sherman Stein, 16:5, 1985, 383-385, 5.1.5, 1.2
- A Babylonian Geometrical Algebra, James K. Bidwell, 17:1, 1986, 22-31, 0.3
- Irrationality Made Easy, Robert Bumcrot, 17:3, 1986, 243-244, C

- The Change of Base Formula for Logarithms, Chris Freiling, 17:5, 1986, 413, C, 5.3.2
- A Guide to Computer Algebra Systems, John M. Hosack, 17:5, 1986, 434-441, 4.1, 5.1.2, 5.1.5, 5.2.3, 5.2.4, 5.2.5
- Behold! The Graphs of  $f$  and  $f$  inverse are Reflections about the Line  $y=x$ , Ayoub B. Ayoub, 18:1, 1987, 52, C, 5.3.2
- Powers and Roots by Recursion, Joseph F. Aieta, 18:5, 1987, 411-416, 0.7, 6.3
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- FFF #7. An Exponential Equation, Ed Barbeau, 20:4, 1989, 317, F (also 20:5, 1989, 404)
- Quick Function Evaluation, Daniel S. Yates, 21:1, 1990, 51, C, 5.1.5
- FFF #25. Solving an Inequality, Ed Barbeau, 21:4, 1990, 303, F
- Geometrical and Graphical Solutions of Quadratic Equations, E. John Hornsby, Jr., 21:5, 1990, 362-369, 0.4
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- FFF #38. How to Solve a Quadratic Equation, Ed Barbeau, 22:2, 1991, 132, F (also 24:4, 1993, 345 and 25:4, 1994, 310)
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- FFF #49. Two Transcendental Equations, Ed Barbeau, 23:1, 1992, 36, F, 5.3.2
- FFF #52. An Application of the Cauchy-Schwartz Inequality, Ed Barbeau, 23:2, 1992, 142, F, 9.5
- Infinitely Many Different Quartic Polynomial Curves, Nitsa Movshovitz-Hader and Alla Shmukler, 23:3, 1992, 186-195, 0.7
- The Joy of Mathematics: A Mary P. Dolciani Lecture, Peter Hilton, 23:4, 1992, 274-281, 1.2
- A Serendipitous Application of the Pythagorean Triplets, Susan Forman, 23:4, 1992, 312-314, C, 9.3
- Commutativity of Polynomials, Shmuel Avital and Edward Barbeau, 23:5, 1992, 386-395, 6.3, 0.7
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- FFF #58. A Rational Combination of Two Transcendentals, Ed Barbeau, 24:3, 1993, 229, F, 5.3.2
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- FFF #60. A Two-Valued Function, Ed Barbeau, 24:3, 1993, 230, F, 5.3.2
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- FFF #67. A Superficial Volume Problem, Randall K. Campbell-Wright, 25:1, 1994, 35, F
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- Approaches to the Formula for the  $n$ th Fibonacci Number, Russell Jay Hendel, 25:2, 1994, 139-142, C, 4.5, 5.4.2, 9.3, 9.5
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- FFF #86. Watch Your Ears!, Bruce Yoshiwara, 26:1, 1995, 36, F
- FFF #87. Do You Know How to Split the Atom?, Milt Eisner, 26:1, 1995, 37, F
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- Proof Without Words: The Pythagorean Theorem, John Molokach, 48:5, 2017, 334, C
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- The Centroid as a Nontrivial Area Bisecting Center of a Triangle, Allan Berele and Stefan Catoiu, 49:1, 2018, 27-34, 9.7
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- Dividing the Circle, Pedro J. Freitas and Hugo Tavares, 49:3, 2018, 187-194, 0.6, 5.3.1, 9.3
- A New Angle on the Fermat-Toricelli Point, David Benko and Dan Coroian, 49:3, 2018, 195-199, 5.1.4, 9.7
- Proof Without Words: Elvis Trades Running for Swimming, Li Zhou, 49:5, 2018, 366, C, 5.1.4, 9.10
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#### 0.4 Analytic geometry

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### 1 Mathematics Education

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- Conceptions of Area: In Students and in History, Bronislaw Czarnocha, Ed Dubinsky, Sergio Loch, Vrunda Prabhu, and Draga Vidakovic, 32:2, 2001, 99-109, 5.2.6
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- Lobb's Generalization of Catalan's Parenthesization Problem, Thomas Koshy, 40:2, 2009, 99-107
- $n$ -Card Tricks, Hang Chen and Curtis Cooper 40:3, 2009, 196-201, 9.2
- Reflections on the  $N + k$  Queens Problem, R. Douglas Chatham, 40:3, 2009, 204-210, 4.1, 9.2
- Summations Involving Binomial Coefficients, Hidefumi Katsuura, 40:4, 2009, 275-278
- Bijective Proof Without Words, Martin Griffiths, 41:2, 2010, 100, C

- Deranged Exams, Michael Z. Spivey, 41:3, 2010, 197-202
- Counting Squares to Sum Squares, Duane W. DeTemple, 41:3, 2010, 214-219
- Taking Turns, Brian Hopkins, 41:4, 2010, 289-297, 3.3, 9.4
- The Tower and Glass Marbles Problem, Richard Denman, David Hailey, and Michael Rothenberg, 41:5, 2010, 350-356, 8.1
- The Rascal Triangle, Alif Anggoro, Eddy Liu, and Angus Tulloch, 41:5, 2010, 393-395, 0.1
- Guards, Galleries, Fortresses, and the Octoplex, T. S. Michael, 42:3, 2011, 191-200, 3.1, 9.7
- An Application of Group Theory to Change Ringing, Michele Intermont and Aileen Murphy, 42:3, 2011, 223-228, 9.4
- Student Research Project: Making Change Efficiently, Jack E. Graver, 42:4, 2011, 317-322, 0.1, 5.1.4, 9.9
- Student Research Project: One-dimensional Czedli-type Islands, Eszter K. Horvath, Attila Mader, and Andreja Tepavcevic, 42:5, 2011, 374-378, C, 0.9, 9.2, 9.3
- Averaging Sums of Powers of Integers, Thomas J. Pfaff, 42:5, 2011, 402-403, C, 9.2, 9.3
- Hexaflexagons, Martin Gardner, 43:1, 2012, 2-5, 0.3, 9.2, 9.4, 9.8
- The V-flex, Triangle Orientation, and Catalan Numbers in Hexaflexagons, Ionut E. Iacob, Bruce McLean, and Hua Wang, 43:1, 2012, 6-10, 0.3, 3.1, 5.4.1, 9.2, 9.8
- Cups and Downs, Ian Stewart, 43:1, 2012, 15-19, 4.1, 9.2
- Mad Tea Party Cyclic Partitions, Robert Bekes, Jean Pedersen, and Bin Shao, 43:1, 2012, 25-36, 9.2, 9.3
- The Secretary Problem from the Applicant's Point of View, Darren Glass, 43:1, 2012, 76-81, 7.2
- 30 Years of Bulgarian Solitaire, Brian Hopkins, 43:2, 2012, 135-140, 9.2, 9.3
- Convergence of a Catalan Series, Thomas Koshy and Zhenguang Gao, 43:2, 2012, 141-146, 5.4.2, 9.3
- RATWYT, Aviezri S. Fraenkel, 43:2, 2012, 160-164, 3.1, 9.2
- Ben-Hur Staircase Climbs, John Dodge and Andrew Simoson, 43:4, 2012, 274-284
- Counting Triangles to Sum Squares, Joe DeMaio, 43:4, 2012, 297-303, 3.1
- The Combinatorial Trace Method in Action, Mike Krebs and Natalie C. Martinez, 44:1, 2013, 32-36, 3.1, 4.5, 9.3
- A Family of Identities via Arbitrary Polynomials, Dong Fengming, Ho Weng Kin, and Lee Tuo Yeong, 44:1, 2013, 43-46
- Multi-Peg Tower of Hanoi, Paul Isihara and Doeke Buursma, 44:2, 2013, 110-116, 9.2
- Proof Without Words: An Alternating Sum of Squares, Joe DeMaio, 44:3, 2013, 170, C, 3.1
- Instant Insanity II, Tom Richmond and Aaron Young, 44:4, 2013, 265-272, 3.1, 9.2
- Mancala Matrices, L. Taalman, A. Tongen, B. Warren, F. Wyrick-Flax, and I. Yoon, 44:4, 2013, 273-283, 4.1, 9.2
- Chomp in Disguise, Andrew MacLaughlin and Alex Meadows, 44:4, 2013, 284-292, 9.2
- Tetris Sudoku, Philip Riley and Laura Taalman, 44:4, 2013, 292, C, 9.2
- Boggle Logic Puzzles: Minimal Solutions, Jonathan Needleman, 44:4, 2013, 293-299, 3.1, 9.2
- Domination and Independence on a Triangular Honeycomb Chessboard, Joe DeMaio and Hong Lien Tran, 44:4, 2013, 307-314, 3.1, 9.2
- Are Stupid Dice Necessary?, Frank Bermudez, Anthony Medina, Amber Rosin, and Eren Scott, 44:4, 2013, 315-322, 7.2, 9.2, 9.3
- Power Series for Up-Down Min-Max Permutations, Fiacha Heneghan and T. Kyle Petersen, 45:2, 2014, 83-91, 5.4.3
- Matroids on Groups?, Jeremy S. LeCrone and Nancy Ann Neudauer, 45:2, 2014, 121-128, 3.1, 9.1, 9.4
- Cookie Monster Devours Naccis, Leigh Marie Braswell and Tanya Khovanova, 45:2, 2014, 129-135, 9.2
- On God's Number(s) for Rubik's Slide, Michael A. Jones, Brittany C. Shelton, and Miriam E. Weaverdyck, 45:4, 2014, 267-275, 3.1, 9.2, 9.4
- Chutes and Ladders with Large Spinners, Darcie Connors and Darren Glass, 45:4, 2014, 289-295, 7.2, 9.2
- Mancala as Nim, Whitney Rhianna Fillers, Bill Linderman, and Andrew Simoson, 45:5, 2014, 350-356, 3.3, 9.2, 9.3
- A Prehistory of Nim, Lisa Rougetet, 45:5, 2014, 358-363, 2.2, 9.2

- A Combinatorial Proof of a Theorem of Katsuura, Brian K. Miceli, 45:5, 2014, 365-369, 9.4
- Proof Without Words: Sums of Every Third Triangular Number, Roger B. Nelsen, 46:2, 2015, 98, C, 9.3
- When is the Generating Function of the Fibonacci Numbers an Integer?, Dae S. Hong, 46:2, 2015, 110-112, 9.3
- Sequences of Power Lines, Ricardo Alfaro, 46:2, 2015, 113-120, 0.2, 0.7, 5.1.1, 5.4.1, 9.2, 9.3
- On an Identity Involving Powers of Binomial Coefficients, Ulrich Abel, 46:2, 2015, 138, C
- Proof Without Words: Each But Two Triangular Numbers Is a Sum of Three Triangular Numbers, Roger B. Nelsen, 46:3, 2015, 172, C, 9.2, 9.3
- How to Win at (One-Round) War, Richard E. Chatwin and Dana MacKenzie, 46:4, 2015, 242-253, 4.1, 9.2, 9.5, 9.9
- Candy Crush Combinatorics, Dana Rowland, 46:4, 2015, 255-262, 9.2
- The Uniqueness of Rock-Paper-Scissors-Lizard-Spock, Brian J. Birgen, 46:4, 2015, 270-273, 9.2
- A Magic Trick Leads to an Identity: Some Induction Fun, Robert W. Vallin, 46:4, 2015, 295-298, C, 0.9, 9.2
- Proof Without Words: Centered Triangular Numbers, Roger B. Nelsen, 46:5, 2015, 335, C, 0.2, 9.2, 9.3
- Journal Problems Sections: Modern Challenges and Teaching Tools, Brian D. Beasley and David R. Stone, 46:5, 2015, 336-346, 0.7, 5.2.9, 5.6.1, 6.1, 9.3
- Explicit Form of the Faulhaber Polynomials, Jose Luis Cereceda, 46:5, 2015, 359-363, 5.4.2
- Proof Without Words: Powers of Three and Triangular Numbers, C. David Leach, 47:2, 2016, 120, C
- Lattice Paths and Harmonic Means, Marc Zucker, 47:2, 2016, 121-124
- The Chu-Vandermonde Identity via Leibniz's Identity for Derivatives, Michael Spivey, 47:3, 2016, 219-220, C
- The FA Cup Draw and Pairing Up Probabilities, Patrick Sullivan, 47:4, 2016, 282-292, 7.2, 9.2
- Integral Value of the Generating Functions of Fibonacci and Lucas Numbers, Prapanpong Pongsriiam, 48:2, 2017, 97-101, 9.3
- On the Arithmetic Mean of the Square Roots of the First  $n$  Positive Integers, Mircea Merca, 48:2, 2017, 129-133, 9.3
- Proof Without Words: Sum of a Row in Pascal's Triangle, Angel Plaza, 48:3, 2017, 188, C, 0.2
- Partitioning the Natural Numbers to Prove the Infinitude of Primes, Arpan Sadhukhan, 48:3, 2017, 217-218, C, 9.3
- Minimal Tilings of a Unit Square, Iwan Praton, 48:4, 2017, 242-247, 9.5, 9.7
- UFOs in the game SET: Looking for Airplanes and Spaceships, Jonathan Needleman and Felicia Sciortino, 48:4, 2017, 249-257, 9.1, 9.2, 9.7
- Tiling Squares with Big Holes with L-triominoes, Patrick J. Costello, 48:4, 2017, 259-263, 9.2, 9.7
- Proof Without Words: A Pascal-Like Triangle With Pell Number Row Sums, Angel Plaza, 48:5, 2017, 346, C, 5.4.1, 6.3, 9.3
- Bet(ch)a my Team Wins the Playoffs, Roger W. Johnson, 48:5, 2017, 347-353, 7.2
- Proof Without Words: A Sum Computed by Self-Similarity, Yukio Kobayashi, 49:1, 2018, 10, C, 3.1, 5.4.2
- Proof Without Words: Sum of Squares of Consecutive Fibonacci Numbers, Tim Price, 49:2, 2018, 121, C, 9.3
- Combinatorics: A Very Short Introduction, Robin Wilson and Infinity: A Very Short Introduction, Ian Stewart, 49:2, 2018, 147-152, reviewed by Brian Hopkins, 10
- Five Families Around a Well: A New Look at an Old Problem, Ezra Brown and Matthew Crawford, 49:3, 2018, 162-168, 2.1, 4.1, 4.2
- Strange Spinners and Diversity of Dice in Chutes and Ladders, Erin Frasetto, Michael Gableman, McKenzie Lamb, Tyler Shimek, and Andrea Young, 49:4, 2018, 251-260, 4.7, 7.2, 9.2, 9.10
- Probabilities of Qwirkle Hand Values, 49:4, 2018, 270-276, 7.2, 9.2, 9.10
- Tactile Tools for Teaching: Implementing Knuth's Algorithm for Mastering Mastermind, Thomas M. Fiore, Alexander Lang, and Antonella Perucca, 49:4, 2018, 278-286, 8.1, 9.1, 9.2

- Bringing Calculus into Discrete Math via the Discrete Derivative, Christopher J. Catone, 50:1, 2019, 21-27, 3.3, 5.1.2, 5.1.3, 5.4.1
- A Birthday in St. Petersburg, Enrique Trevino, 50:1, 2019, 36-40, 7.2
- The Barycenter Theorem: Averaging Possible-Paths to Produce Optimal Discrete Straight-line Segments, Robert M. French and Patrick Gehant, 50:2, 2019, 103-114, 8.3, 9.7
- Unfoldings of the Cube, Richard Goldstone and Robert Suzzi Valli, 50:3, 2019, 173-184, 0.3, 3.1, 9.7
- Coloring a 1-by-n Chessboard, Elias Abboud, Rathi Saleh, and Amal-Sharif Rassian, 49:5, 2019, 322-330, 5.4.2, 9.2
- Sums of Powers of Consecutive Integers and Pascal's Triangle, Semyon Litvinov and Frantisek Marko, 51:1, 2020, 25-31, 4.1, 5.2.1, 9.3
- Connected Subsets of an  $n \times 2$  Rectangle, Samuel Durham and Tom Richmond, 51:1, 2020, 32-42, 5.4.1, 8.3, 9.7
- A Fast-Growing Sequence Inspired by TREE( $k$ ), Kevin Y. Du, 51:1, 2020, 43-50, 3.1, 5.4.1
- Randomly Generated Identities, David Treeby, 51:2, 2020, 90-94, 5.4.2, 7.2
- The Proportion of Comets in the Card Game SET, Dan May and Dan Swenson, 51:3, 2020, 162-172, 4.3, 6.3, 7.2, 9.1, 9.2, 9.4
- Counting Connected Sets of Squares, Stan Wagon, 51:3, 2020, 173, 9.7
- Chance Encounters with Large Polynomials, Brian D. Jones, 51:3, 2020, 174-181, 0.2, 7.2
- A Tour of Discrete Probability Guided by a Problem in Genomics, Leonid Hanin, 51:4, 2020, 284-294, 7.2, 9.10
- When Rooks Miss: Probability Through Chess, Stephen J. Miller, Haoyu Sheng & Daniel Turek, 52:2, 2021, 82-93, 5.1.1, 7.2, 7.3, 9.2, 9.10
- Visual Proofs for the Sums of Fourth and Fifth Powers of the First  $n$  Natural Numbers, Sanja Stevanovi & Dragan Stevanovic, 52:2, 2021, 115-120, 5.4.2, 9.3
- Shortest Paths on Cubes, Richard Goldstone, Rachel Roca & Robert Suzzi Valli, 52:2, 2021, 121-132, 0.3, 0.4, 9.7, 9.8
- Visual Triangular Number Identities from Positional Number Systems, Tom Edgar, 52:2, 2021, 133-136, 6.3, 9.3
- Distances Between Factorizations of the Chicken McNugget Monoid, Scott Chapman, Pedro Garcia-Sanchez & Christopher O'Neill, 52:3, 2021, 158-176, 3.1, 9.2, 9.4
- The Sock Problem Revisited, William Paulsen, 52:3, 2021, 193-203, 3.1, 5.4.1, 6.3, 7.2, 9.6
- An Unusual Recursive Formula to Answer a Question Regarding Fixed Points in Permutations, Melanie Tian & Enrique Trevino, 52:3, 2021, 219-220, C, 6.3, 7.2
- Parking Functions: Choose Your Own Adventure, Joshua Carlson, Alex Christensen, Pamela E. Harris, Zakiya Jones & Andrés Ramos Rodríguez, 52:4, 2021, 254-26, 7.2, 9.2
- Back to the Tower, John P. Bonomo, 52:4, 2021, 265-273, 6.3, 9.2
- Fano, Galois, Hamming and a Card Trick, Richard Ehrenborg, 52:4, 2021, 274-280, 9.2, 9.4, 9.7
- Counting Christmas Trees, Tiffany N. Kolba and Jonathan Beagley, 52:5, 2021, 338-344, 3.1
- Arranging Beetles, Robert Gallant & Georg Gunther, 53:1, 2022, 3-12, 3.1, 9.2
- Report on the 12<sup>th</sup> Annual USA Junior Mathematical Olympiad, Bela Bajnok & Evan Chen, 53:1, 2022, 13-20, 0.3, 5.4.1, 9.1, 9.2, 9.3, 9.5
- Connections Between Partitions and Divisors Related to the Parity of the Partition Function, Mircea Merca, 53:1, 2022, 33-37, 9.3
- On the Sum of  $k$ -th Powers in Terms of Earlier Sums, Steven J. Miller & Enrique Trevino, 53:3, 2022, 220-225, 9.3

### 3.3 Other topics in discrete mathematics (also see 6.3)

- Who Stole the Apples and The Sticks?, Ross Honsberger, 10:1, 1979, 30-32, 3.1
- Computer-Generated Knight Tours, Michael Gilpin, 13:4, 1982, 252-259, 3.1, 9.2
- Drawing the Line Segment Connecting Two Points, Harley Flanders, 18:1, 1987, 53-57, 0.4, 8.1

Card Shuffling in Discrete Mathematics, Steve M. Cohen and Paul R. Coe, 26:3, 1995, 224-227, C, 9.4  
Exploring Fibonacci Numbers Mod M, Jack Ryder, 27:2, 1996, 122-124, C, 9.3  
A Better Draft: Fair Division of the Talent Pool, Bryan Dawson, 28:2, 1997, 82-88  
Putting the Pieces Together: Understanding Robinson's Nonperiodic Tilings, Aimee Johnson and Kathleen Madden, 28:3, 1997, 172-181, 0.3  
Weighing Coins: Divide and Conquer to Detect a Counterfeit, Mario Martelli and Gerald Gannon, 28:5, 1997, 365-367, 0.9  
A Discrete Intermediate Value Theorem, Richard Johnsonbaugh, 29:1, 1998, 42, C, 0.9  
FFF #134. Hockey Ranking, Dave Trautman, 29:5, 1998, 406-407, F  
Recursion in Action, Peter Ross, 31:1, 2000, 68, C  
Ten into Eight Won't Go?, Marc Brodie, 32:4, 2001, 296, C  
In Search of a Missing Link: A Case Study in Error-Correcting Codes, Andy Liu, 32:5, 2001, 343-347  
Centering, Jim Sauerberg and Alan Tarr, 33:1, 2002, 24-31, 0.4, 6.3  
Miscellanea: A Ballot Count Surprise, N. S. Mendelsohn, 33:5, 2002, 431-432, C, 7.2  
Apportionment and the 2000 Election, Michael G. Neubauer and Joel Zeitlin, 34:1, 2003, 2-10  
Simmons' Subliminal Channel, Hector Rosario, 35:3, 2004, 208-212  
A Geometric Approach to Fair Division, Julius Barbanel, 41:4, 2010, 268-280, 9.5, 9.7  
Taking Turns, Brian Hopkins, 41:4, 2010, 289-297, 3.2, 9.4  
Who Does the Housework?, Angela Vierling-Claassen, 41:4, 2010, 298-302  
Lewis Carroll, Voting, and the Taxicab Metric, Thomas C. Ratliff, 41:4, 2010, 303-311, 0.3, 3.1  
Visualizing Elections using Saari Triangles, Mariah Birgen, 41:4, 2010, 325-328, 0.1, 0.3  
A Talmudic Fair-Division Problem, Theodore Hill, 41:4, 2010, 338, C, 0.1  
Two-Person Pie-Cutting: The Fairest Cuts, Julius B. Barbanel and Steven J. Brams, 42:1, 2011, 25-32  
Retrolife and the Pawns Neighbors, Yossi Elran, 43:2, 2012, 147-151, 9.2, 9.10  
Lake Wobegon Dice, Jorge Moraleda and David G. Stork, 43:2, 2012, 152-159, 7.2, 9.2, 9.9  
Mancala as Nim, Whitney Rhianna Fillers, Bill Linderman, and Andrew Simoson, 45:5, 2014, 350-356,  
3.2, 9.2, 9.3  
Balanced Nontransitive Dice, Alex Schaefer and Jay Schweig, 48:1, 2017, 10-16, 7.1, 7.2, 9.2  
The Solution to a Hanoi-ing Little Problem, John P. Bonomo, 49:4, 2018, 288-291, 6.3, 8.1, 9.2  
Bringing Calculus into Discrete Math via the Discrete Derivative, Christopher J. Catone, 50:1, 2019, 21-  
27, 3.2, 5.1.2, 5.1.3, 5.4.1  
A Plea for Finite Calculus, Michael Schmitz, 52:2, 2021, 94-105, 1.1, 2.2, 5.1.2

### 3.4 Software for discrete mathematics

A Mathematics Software Database, R. S. Cunningham and David A. Smith, 17:3, 1986, 255-266, 0.10,  
4.8, 5.8, 6.7, 7.4, 9.11  
A Mathematics Software Database Update, R. S. Cunningham and David A. Smith, 18:3, 1987, 242-247,  
0.10, 4.8, 5.8, 6.7, 7.4, 9.11  
The Compleat Mathematics Software Database, R. S. Cunningham and David A. Smith, 19:3, 1988, 268-  
289, 0.10, 4.8, 5.8, 6.7, 7.4, 9.11  
EDUCOM Higher Education Software Awards for 1991: Combinatorica@, Bruce E. Sagan, 23:4, 1992,  
334-339, 3.2  
Using PROLOG in Discrete Mathematics, Antonio M. Lopez, Jr., 24:4, 1993, 357-365, 3.1, 9.1  
Forget Not the Lowly Spreadsheet, Michael G. Henle, 26:4, 1995, 320-328, 6.7  
Fibonacci Powers and a Fascinating Triangle, Dale K. Hathaway and Stephen L. Brown, 28:2, 1997, 124-  
128, C, 6.3, 9.3

## 4 Linear Algebra

### 4.1 Matrices, systems of linear equations, and matrix algebra

- Mathematics, A Solitary Game, Olof Hanner, 1:2, 1970, 5-16, 0.2
- On One-Sided Inverses of Matrices, Elmar Zemgalis, 2:1, 1971, 45-48
- On Transformations and Matrices, Marc Swadener, 4:3, 1973, 44-51, 4.4
- Computer-Generated Problem Sets: Simultaneous Equations and Matrices, Samuel W. Spero and Mary Koehler, 8:3, 1977, 182-187
- Binomial Matrices, Jay E. Strum, 8:5, 1977, 260-266
- Integer Matrices Whose Inverses Contain Only Integers, Robert Hanson, 13:1, 1982, 18-21
- Mathematics in Archaeology, Gareth Williams, 13:1, 1982, 56-58, C
- The Mathematics of Tucker: A Sampler, Albert W. Tucker, 14:3, 1983, 228-232
- Basic Null Space Calculations, Dan Kalman, 15:1, 1984, 42-47
- The Electronic Spreadsheet and Mathematical Algorithms, Deane E. Arganbright, 15:2, 1984, 148-157, 5.4.1, 7.3, 9.6
- Visual Thinking about Rotations and Reflections, Tom Brieske, 15:5, 1984, 406-410, 4.4
- Classifying Row-reduced Echelon Matrices, Stewart Venit and Wayne Bishop, 17:2, 1986, 169-170, C
- Self-Inverse Integer Matrices, Robert Hanson, 16:3, 1985, 190-198
- Using Minitab in Linear Algebra, Raymond N. Greenwell, 16:3, 1985, 216-218
- Harvesting a Grizzly Bear Population, Michael Caulfield and John Kent and Daniel McCaffrey, 17:1, 1986, 34-46, 4.6, 9.10
- Teaching Mathematics Using APL, Edward J. LeCuyer, Jr., 17:4, 1986, 344-357
- On Polynomial Matrix Equations, Harley Flanders, 17:5, 1986, 388-391, 4.5
- A Guide to Computer Algebra Systems, John M. Hosack, 17:5, 1986, 434-441, 0.2, 5.1.2, 5.1.5, 5.2.3, 5.2.4, 5.2.5
- Why Should We Pivot in Gaussian Elimination?, Edward Rozema, 19:1, 1988, 63-72, 4.6
- Notational Collisions, J. Hillel, 20:5, 1989, 418-422, C, 1.2
- Minimum Dimension for a Square Matrix of Order n, Robert Hanson, 21:1, 1990, 28-34, 9.4
- A Tool for Teaching Linear Programming within MATLAB, David R. Hill, 21:1, 1990, 55-56, C, 9.9
- Software Review: Linear Algebra Software for the IBM PC, David P. Kraines and Vivian Y. Kraines, 21:1, 1990, 57-64, 4.8
- FFF #16. Nonsquare Invertible Matrices, Ed Barbeau, 21:2, 1990, 127, F (also 22:3, 1991, 223 and 23:3, 1992, 204)
- A Zero-Row Reduction Algorithm for Obtaining the gcd of Polynomials, Sidney H. Kung and Yap S. Chua, 21:2, 1990, 138-141, 0.7, 9.4
- Elementary Row Operations and LU Decomposition, David P. Kraines and Vivian Y. Kraines and David A. Smith, 21:5, 1990, 418-419, C
- Rotations in Space and Orthogonal Matrices, David P. Kraines, 22:3, 1991, 245-247, C, 4.3, 4.4, 4.5
- Number Theory and Linear Algebra: Exact Solutions of Integer Systems, George Mackiw, 23:1, 1992, 52-58, 9.3
- Gems of Exposition in Elementary Linear Algebra, David Carlson and Charles R. Johnson and David Lay and A. Duane Porter, 23:4, 1992, 299-303, 1.2, 4.5, 4.7
- A Random Ladder Game: Permutations, Eigenvalues, and Convergence of Markov Chains, Lester H. Lange and James W. Miller, 23:5, 1992, 373-385, 4.5, 9.10
- Graphs, Matrices, and Subspaces, Gilbert Strang, 24:1, 1993, 20-28, 3.1, 4.3
- Teaching Linear Algebra: Must the Fog Always Roll In?, David Carlson, 24:1, 1993, 29-40, 1.2
- The Linear Algebra Curriculum Study Group Recommendations for the First Course in Linear Algebra, David Carlson and Charles R. Johnson and David C. Lay and A. Duane Porter, 24:1, 1993, 41-46, 1.2, 4.2, 4.3, 4.5
- Linear Algebra and Affine Planar Transformations, Gerald J. Porter, 24:1, 1993, 47-51, 0.4, 4.4
- FFF. Matrices and the TI-81 Graphics Calculator, Constance J. Gardner, 24:1, 1993, 64, F, 0.2
- Gaussian Elimination in Integer Arithmetic: An Application of the L-U Factorization, Thomas Hern, 24:1, 1993, 67-71, C

- Iterative Methods in Introductory Linear Algebra, Donald R. LaTorre, 24:1, 1993, 79-88, 4.5, 9.6
- Software Review: Spreadsheets in Linear Algebra, Deane Arganbright, 24:1, 1993, 89-94, 4.8
- How Does the NFL Rate the Passing Ability of Quarterbacks?, Roger W. Johnson, 24:5, 1993, 451-453, C (also 25:4, 1994, 340)
- Using Computer Algebra Systems to Teach Linear Algebra (software review), Maurino P. Bautista, 24:5, 1993, 462-471, 4.5, 4.8
- Round-off, Batting Averages, and Ill-Conditioning, Edward Rozema, 25:4, 1994, 314-317, C, 4.6
- Matrix Patterns and Underdetermined Coefficients, Herman Gollwitzer, 25:5, 1994, 444-448, C, 6.2
- For matrices: AB transpose equals B transpose times A transpose (proof by picture), James G. Simmonds, 26:3, 1995, 250, C
- Linear Algebra on the Gridiron, Daniel C. Isaksen, 26:5, 1995, 358-360
- Using the *College Mathematics Journal* Topic Index in Undergraduate Courses, Donald E. Hooley, 28:2, 1997, 106-109, 4.2, 5.1.4, 5.7.1
- FFF #114. An Inversion Conundrum, Barry D. Ganapol, 28:2, 1997, 120, F
- A Diagonal Perspective on Matrices, Eugene C. Boman and Margaret A. Misconish, 29:1, 1998, 37-38, C
- Using Consistence Condition to Solve Linear Systems, Geza Schay, 30:3, 1999, 226-229, C
- N-Site Insights, Bret Draayer, 31:4, 2000, 250-258, 5.5
- FFF #172. Creating an idempotent, Douglas W. Mitchell, 32:1, 2001, 50, F
- The Profit in Being Unbalanced, Wolf von Ronik, 32:5, 2001, 348-351, 0.8
- A Ramanujan Result Viewed From Matrix Algebra, Raymond A. Beauregard and E. R. Suryanarayanan, 33:3, 2002, 212-214, 9.3, 9.4
- When is  $1/(a-b) = 1/a + 1/b$ , Anyway?, Eugene Boman and Frank Uhlig, 33:4, 2002, 296-300, 9.5
- Obtaining the QR Decomposition by Pairs of Row and Column Operations, Sidney H. Kung, 33:4, 2002, 320-321, C, 4.6
- An Underdetermined Linear System for GPS, Dan Kalmar, 33:5, 2002, 384-390
- FFF. Matrix Inverses and the Great Injustice, Zoran Sunik, 33:5, 2002, 395-398, F
- Parrondo's Paradox – Hope for Losers!, Darrell P. Minor, 34:1, 2003, 15-20, 7.2
- On the Square Root of  $aa^T + bb^T$ , Dietrich Trenkler and Gotz Trenkler, 34:1, 2003, 39-41
- A Class of Exponential Matrices, M. A. Khan, 34:3, 2003, 194-195
- The Chain Rule for Matrix Exponential Functions, Jay A. Wood, 35:3, 2004, 220-222, C
- The Cross Product as a Polar Decomposition, Gotz Trenkler, 39:3, 2008, 237-239, C, 4.3, 5.5
- Reflections on the  $N + k$  Queens Problem, R. Douglas Chatham, 40:3, 2009, 204-210, 3.2, 9.2
- Finding Matrices that Satisfy Functional Equations, Scott Duke Kominers, 40:4, 2009, 289-292, C, 5.4.3
- Student Research Project: Golden Matrix Families, Anne Fontaine and Susan Hurley, 42:2, 2011, 140-147, 4.5, 9.4
- The Easiest Lights Out Games, Bruce Torrence, 42:5, 2011, 361-371, 4.3, 9.2
- Cups and Downs, Ian Stewart, 43:1, 2012, 15-19, 3.2, 9.2
- Push-To Telescope Mathematics, Donald Teets, 43:3, 2012, 227-231, 4.4
- Asset Pricing, Financial Markets, and Linear Algebra, Marcio Diniz, 44:1, 2013, 2-8, 4.3, 7.2, 9.9
- Teaching Tip: When a Matrix and Its Inverse Are Stochastic, J. Ding and N. H. Rhee, 44:2, 2013, 108-109, C
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## 5 Calculus

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## 5.2 Integration

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- Reaction to Responses to "Should Mathematicians Teach Statistics?", David S. Moore, 19:1, 1988, 32-34, 1.2
- Readers' Responses to the January 1988 Forum: "Should Mathematicians Teach Statistics?", Joseph B. Kadane and William A. Golomsky and Daniel A. Sankowsky and Benjamin M. Perles, 19:2, 1988, 164-165, 1.2
- Theory, Simulation and Reality, Peter Flusser, 19:3, 1988, 210-222, 9.10, 7.2
- Using Leverage and Influence to Introduce Regression Diagnostics, David C. Hoaglin, 19:5, 1988, 387-401
- Conditional Expectations and the Correlation Function, Barthel W. Huff, 20:1, 1989, 55-57, C
- A Note on Pascal's Triangle and Simple Random Sampling, Tommy Wright, 20:1, 1989, 59-66
- Using Median Splits to Motivate Learning, David P. Doane, 20:3, 1989, 228-229, C
- Sensitive Questions and Randomized Response Techniques, Kenneth R. Kundert, 20:5, 1989, 409-411, C
- The Longest Run of Heads, Mark F. Schilling, 21:3, 1990, 196-207
- Bernoulli Trials and the Central Limit Theorem, David P. Kraines and Vivian Y. Kraines and David A. Smith, 21:5, 1990, 415-416, C
- Using Simulation to Study Linear Regression, LeRoy A. Franklin, 23:4, 1992, 290-295, 9.10
- Least Squares and Quadric Surfaces, Donald Teets, 24:3, 1993, 243-244, C, 5.7.1, 5.6.2
- Determining Sample Sizes for Monte Carlo Integration, David Neal, 24:3, 1993, 254-262, C, 5.2.2, 9.10
- Quadratic Confidence Intervals, Neil C. Schwertman and Larry R. Dion, 24:5, 1993, 453-457, C

- Chebyshev's Theorem: A Geometric Approach, Pat Touhey, 26:2, 1995, 139-141, C
- MAD Property of Medians: An Induction Proof, Eugene F. Schuster, 26:5, 1995, 387-389, C, 0.9
- Will the Real Best Fit Curve Please Stand Up?, Helen Skala, 27:3, 1996, 220-223, C, 5.7.1
- What is the Margin of Error of a Poll?, Bennett Eisenberg, 28:3, 1997, 201-203, C
- Student's t and Crackers, Paul M. Sommers, 30:1, 1999, 32-34
- Recommendations for Teaching the Reasoning of Statistical Inference, Allan Rossman and Beth Chance, 30:4, 1999, 297-305, 1.1
- Getting Normal Probability Approximations Without Using Normal Tables, Peter Thompson and Lorrie Lendvoy, 31:1, 2000, 51-54, C
- The Super Bowl Theory: Fourth and Long, Paul Sommers, 31:3, 2000
- The Geometry of Statistics, David Farnsworth, 31:3, 2000, 200-204
- t-Probabilities as Finite Sums, Neil Eklund, 31:3, 2000, 217-218, C
- The Lognormal Distribution, Brian E. Smith and Francis Merceret, 31:4, 2000, 259-261
- Food and Drug Interaction: What Role Does Statistics Play?, Thomas Bradstreet, 31:4, 2000, 268-273
- Well-Rounded Figures, Yves Nievergelt, 32:1, 2001, 30-32, 9.6
- The Average Speed on the Highway, Larry Clevenson, Mark Schilling, Ann Watkins, and William Watkins, 32:3, 2001, 169-171
- Is Presidential Greatness Related to Height?, Paul M. Sommers, 33:1, 2002, 14-16
- Symmetric or Skewed?, Joseph G. Eisenhauer, 33:1, 2002, 48-51, C
- Winning Games in Canadian Football: A Logistic Regression Analysis, Keith A. Willoughby, 33:3, 2002, 215-220
- Almost-Binomial Random Variables, Peter Thompson, 33:3, 2002, 235-237, C
- Chasing Hank Aaron's Home Run Record, Steven P. Bisgaier, Benjamin S. Bradley, Peter D. Harwood, and Paul M. Sommers, 33:4, 2002, 293-295
- Observations on the Indeterminacy of the Sample Correlation Coefficient, Owen Byer, 33:4, 2002, 316-318, C
- Baseball's All-Stars: Birthplace and Distribution, Paul M. Sommers, 34:1, 2003, 24-30
- A Calculus Theorem Motivated by a Statistics Problem, David L. Farnsworth, 35:2, 2004, 126-129, C
- FFF. Teenagers, Sex and Accidents, Joseph G. Eisenhauer, 35:3, 2004, 213-214, F
- A Quick Proof that the Least Squares Formulas Give a Local Minimum, W. M. Dunn III, 36:1, 2005, 64-65, C, 5.7.1
- A Painless Approach to Least Squares, Eric S. Key, 36:1, 2005, 65-67, C
- A Recursive Formula for Moments of a Binomial Distribution, Arpad Benyi and Saverio M. Manago, 36:1, 2005, 68-72, C
- The Sample Correlation Coefficient from a Linear Algebra Perspective, C. Ray Rosentrater, 37:1, 2006, 47-50, C, 4.3
- An Elegant Mode for Determining the Mode, D. S. Broca, 37:2, 2006, 134-137, C
- FFF #252. A snafu, Kenneth Schilling, 37:4, 2006, 290, F
- Distortion of average class size: The Lake Wobegon effect, Allen Schwenk, 37:4, 2006, 293-296, C
- More Mathematics in the Bedroom: A Paradoxical Probability, Paul K. Stockmeyer, 38:5, 2007, 339-344, 9.4
- A Waiting-Time Surprise, Richard Parris, 39:1, 2008, 59-63, C
- The Pearson and Cauchy-Schwarz Inequalities, David Rose, 39:1, 2008, 64, C, 5.5, 9.5
- Average Perceived Class Size and Average Perceived Population Density, Clifford H. Wagner, 40:4, 2009, 284-287, C
- Teaching Tip: The Median is a Balance Point, Mark Lynch, 40:4, 2009, 292, C
- Correlation of the Union of Two Bivariate Data Sets, Robert A. Fontenot, 40:5, 2009, 370-373, C
- An Upper Bound for the Expected Range of a Random Sample, Manuel Lopez and James Marengo, 41:1, 2010, 42-48
- The Distribution of the Sum of Signed Ranks, Brian Albright, 43:3, 2012, 232-236
- Suspense at the Ballot Box, Nat Kell and Matt Kretchmar, 44:1, 2013, 9-16, 7.2, 9.10

- Gender Bias?, Elizabeth A. Burroughs and Jessica M. Deshler, 44:2, 2013, 88, C
- Quiz Today: Should I Skip Class?, Peter Zizler, 44:3, 2013, 166-170
- Seasonal Variation in Epidemiology, Osvaldo Marrero, 44:5, 2013, 386-398, 9.10
- Student Research Project: About the Pace of Climate Change: Write a Report to the President, Lily Khadavi, 44:5, 2013, 428-432, C, 5.1.5, 9.10
- Calculus from a Statistics Perspective, Kimberly Leung, Chris Rasmussen, Samuel S. P. Shen, and Dov Zazkis, 45:5, 2014, 377-386, 5.1.2, 5.2.1
- Predicting Wins and Losses: A Volleyball Case Study, Elizabeth Knapper and Hope McIlwain, 46:5, 2015, 352-358, 4.1, 9.10
- Simplified Expectations in the Birthday Problem, Leonard Littleton and Russell May, 47:1, 2016, 50-55, 5.3.4, 5.4.3
- Empirical Modeling: Choosing Models and Fitting Them to Data, Glenn Ledder, 47:2, 2016, 109-119, 9.10
- Statistics on the Bonus Round of Wheel of Fortune, Kathleen Ryan and Brittany Shelton, 47:4, 2016, 250-253, 7.3, 9.2
- Covariances Between Transient States in finite Absorbing Markov Chains, Michael A. Carchidi and Robert L. Higgins, 48:1, 2017, 42-50, 9.9
- A Very Short Proof that the Sum of Independent Normal Random Variables Is Normal, Bennett Eisenberg, 48:2, 2017, 137, C
- A Curious Feature of Regression, Carl V. Lutzer, 48:3, 2017, 189-198, 4.1
- A Riemann Sum Approach to Buffon's Needle, Stephen Kaczkowski, 50:2, 2019, 93-102, 5.2.1, 7.2
- The Choking Index: An Analysis of Performance Under Pressure on the PGA Tour, William W. Miles and Sammi E. Smith, 49:4, 2019, 260-271, 9.2
- A Two-Dimensional Perspective on Simpson's Paradox and Its Likelihood, Michael A. Jones, 49:4, 2019, 295-297, C, 0.4, 9.2, 9.10
- Modeling Emergency Room Arrivals Using the Poisson Process, Lindsey Bell and Rachel Wagner, 49:5, 2019, 343-350, 7.2, 9.10
- To Replace or Not to Replace – That is the Question, John Engbers and Adam Hammett, 51:2, 2020, 117-123, 7.2
- Extremal Correlation Coefficients for Bivariate Probability Distributions with Specified Marginal Distributions, Anurag Agarwal, David L. Farnsworth, Carl V. Lutzer, James E. Marengo, and J. A. Stephen Viggiano, 52:1, 2021, 45-53
- When Rooks Miss: Probability Through Chess, Stephen J. Miller, Haoyu Sheng & Daniel Turek, 52:2, 2021, 82-93, 3.2, 5.1.1, 7.2, 9.2, 9.10
- Statistical Significance of the Median of a Set of Points on the Plane, Antonio J. Moreno Verdejo, Abraham Lopez Viveros & Rafael Ramirez Ucles, 52:3, 2021, 205-218, 0.3, 0.4, 9.7
- Proof Without Words: Convex Hulls and Jensen's Inequality, Dennis L. Sun, 52:4, 2021, 298, C, 9.5
- Optimal Pooling of COVID-19 Samples, Edward A. Roualdes and Neil C. Schwertman, 52:5, 2021, 380-384, 5.1.4
- Correlation and Subtraction, Hanumant Singh Shekhawat, 53:3, 2022, 233-234, C

#### 7.4 Software for probability and statistics

- A Mathematics Software Database, R. S. Cunningham and David A. Smith, 17:3, 1986, 255-266, 0.10, 3.4, 4.8, 5.8, 6.7, 9.11
- A Mathematics Software Database Update, R. S. Cunningham and David A. Smith, 18:3, 1987, 242-247, 0.10, 3.4, 4.8, 5.8, 6.7, 9.11
- The Compleat Mathematics Software Database, R. S. Cunningham and David A. Smith, 19:3, 1988, 268-289, 0.10, 3.4, 4.8, 5.8, 6.7, 9.11
- Software Reviews: *Activstats*, Norman Preston, 32:2, 2001, 138-140

SAGE: Open Source Mathematics Software System, reviewed by J. K. Denny, 44:2, 2013, 149-155, C, 4.8, 5.8, 6.7, 9.11  
Statistics Web Apps, Anne Quinn, 48:5, 2017, 378-382

## 8 Computer Science

### 8.1 Programming and algorithms

Drawing the Line Segment Connecting Two Points, Harley Flanders, 18:1, 1987, 53-57, 0.4, 3.3  
Enhancing the Value of Graphics Programs, Clifford H. Wagner, 18:2, 1987, 142-152, 8.3  
Controlling Roundoff Errors in Sums, Harley Flanders, 18:2, 1987, 153-156, 9.6  
Computing Pi, Harley Flanders, 18:3, 1987, 230-235, 5.2.3, 5.4.2  
Fibonacci Numbers and Computer Algorithms, John Atkins and Robert Geist, 18:4, 1987, 328-336, 5.1.4, 6.3  
Computing nth Roots, Keith Mathews, 19:2, 1988, 174-176  
Sieving Primes on a Micro, Harley Flanders and Alan F. Tomala, 19:4, 1988, 364-367, 9.3  
How Mathematicians Know What Computers Can't Do, Leon Harkleroad, 27:1, 1996, 37-42  
CORDIC: Elementary Function Computation Using Recursive Sequences, Neil Eklund, 32:5, 2001, 330-333, 9.6  
FFF #234. Multiplication algorithms, Yves Nievergelt, 39:2, 2008, 137-138, F, 0.1  
The Tower and Glass Marbles Problem, Richard Denman, David Hailey, and Michael Rothenberg, 41:5, 2010, 350-356, 3.2  
Winning a Pool is Harder Than You Thought, John P. Bonomo, 47:5, 2016, 347-354  
Tactile Tools for Teaching: Implementing Knuth's Algorithm for Mastering Mastermind, Thomas M. Fiore, Alexander Lang, and Antonella Perucca, 49:4, 2018, 278-286, 3.2, 9.1, 9.2  
The Solution to a Hanoi-ing Little Problem, John P. Bonomo, 49:4, 2018, 288-291, 3.3, 6.3, 9.2

### 8.2 Data structures

Generating Posets, Harley Flanders, 18:4, 1987, 323-327, 9.4  
The Flowering of String Rewriting Systems, Anne M. Burns, 23:3, 1992, 225-235, 8.3

### 8.3 Computer graphics

Enhancing the Value of Graphics Programs, Clifford H. Wagner, 18:2, 1987, 142-152, 8.1  
Drawing a Circle, Harley Flanders, 19:1, 1988, 72-78  
Parametric Surfaces, Harley Flanders, 19:5, 1988, 444-447, 5.6.1  
The Curious Fate of an Applied Problem, Alan H. Schoenfeld, 20:2, 1989, 115-123, 5.1.5, 9.5  
The Matrix of a Rotation, Roger C. Alperin, 20:3, 1989, 230, C, 4.3  
Image Expansion in Integer Arithmetic, Mark Bridger, 22:5, 1991, 429-435  
Calculus and Computer Vision, Mark Bridger, 23:2, 1992, 132-141, 5.7.1  
The Flowering of String Rewriting Systems, Anne M. Burns, 23:3, 1992, 225-236, 8.2  
Fireworks, J. M. A. Danby, 23:3, 1992, 237-240, C, 6.2  
Complex Vectors and Image Identification, Lyndell Kerley and Jeff Knisley, 24:2, 1993, 166-174, 9.6  
A Computer Lab for Multivariate Calculus, Casper R. Curjel, 24:2, 1993, 175-177, C, 1.2, 5.7.1  
Making Mountains from a Sum of Molehills, Anne M. Burns, 26:1, 1995, 51-57  
Modeling Trees with a Stochastic Matrix, Anne M. Burns, 29:3, 1998, 230-236, 3.1  
Breaking the Holiday Inn Priority Club CAPTCHA, Edward Aboufadel, Julia Olsen, and Jesse Windle, 36:2, 2005, 101-108, 4.7, 9.10  
The Barycenter Theorem: Averaging Possible-Paths to Produce Optimal Discrete Straight-line Segments, Robert M. French and Patrick Gehant, 50:2, 2019, 103-114, 3.2, 9.7

Fitting a Cubic Bezier to a Parametric Function, Alvin Penner, 50:3, 2019, 185-196, 5.5, 5.6.1, 5.7.3, 5.8, 9.6

Connected Subsets of an  $n \times 2$  Rectangle, Samuel Durham and Tom Richmond, 51:1, 2020, 32-42, 3.2, 5.4.1, 9.7

Visualizing the Complex Roots of Quadratic and Cubic Polynomial Functions in Three Dimensions, Aniket Sanghi, 52:5, 2021, 373-379, 0.7, 5.1.5, 9.6

#### 8.4 Other topics in computer science

Of Memories, Neurons, and Rank-One Corrections, Kevin G. Kirby, 28:1, 1997, 2-19, 4.6

Riemann Sums for Generalized Integrals, Jean-Paul Truc, 50:2, 2019, 123-132, 5.2.1, 5.2.9, 5.2.10, 5.4.2

Idempotent Factorizations in the Cryptography Classroom, Barry S. Fagin, 51:3, 2020, 195-203, 9.3

### 9 Other Topics

#### 9.1 Set theory and logic (also see 0.9)

If...Some Suggestions on Presenting the Connector "if...then", Aaron Seligman, 1:2, 1970, 22-26, 0.9  
Factoring Functions, J. C. Bodenrader, 2:1, 1971, 23-26, 0.6, 5.1.2, 3.2

Some Applications of the Law of the Contrapositive, Morton J. Hellman, 4:3, 1973, 86-88, C, 0.9

The Equivalence of the Well-Ordering Principle and Dirichlet's Box Principle, Aron Pinker, 5:1, 1974, 76-77, C

Who Dunnit?, Lawrence G. Gilligan and Robert B. Nenno, 5:1, 1974, 78-79, C

Godel's Theorem (Part I), Richard Wiebe, 6:2, 1975, 13-17

Godel's Theorem (Part II), Richard Wiebe, 6:3, 1975, 4-7

Mathematics—Is It Any of Your Business?, Ralph Mansfield, 6:3, 1975, 20-26, 3.1, 1.2

Solving Whodunits by Symbolic Logic, Lawrence Sher, 6:4, 1975, 36-38

On the Definition of Implication: Classroom Discussion and Justification, Ray F. Snipes, 8:4, 1977, 247-252, C

Types of Relations, Kenneth Slonneger, 8:5, 1977, 267-269

Boolean Algebra as a Proof Paradigm, Lawrence Sher, 9:3, 1978, 186-190

Analogies and Metaphors to Explain Godel's Theorem, Douglas R. Hofstadter, 13:2, 1982, 98-114

A Machine as Smart as God, Rudy Rucker, 13:2, 1982, 115-121, 2.2

The Asylum of Doctor Tarr and Professor Fether, Raymond Smullyan, 13:2, 1982, 142-146

Probabilistic Dependence Between Events, Ruma Falk and Maya Bar-Hillel, 14:3, 1983, 240-247, 7.2

A Computational Approach to Logical Statements, J. N. Boyd and P. N. Raychowdhury, 14:4, 1983, 326-341

Is the Venn Diagram Good Enough?, Mou-Liang Kung and George C. Harrison, 15:1, 1984, 48-50, 0.2

The Construction of Venn Diagrams, Branko Grunbaum, 15:3, 1984, 238-247

An Odd Induction Proof, Karl David, 15:3, 1984, 251, C

How to Live to be 100, Robert Geist, 15:4, 1984, 256-263

On Venn Diagrams and the Counting of Regions, Branko Grunbaum, 15:5, 1984, 433-435, C

Satan, Cantor, and Infinity, Raymond M. Smullyan, 16:2, 1985, 118-121

FFF #9. The Countability of the Reals, Ed Barbeau, 20:5, 1989, 403, F, 9.5 (also 21:1, 1990, 36 and 22:5, 1991, 405)

FFF # 10. The Uncountability of the Plane, Ed Barbeau, 20:5, 1989, 403-404, F, 9.5 (also 21:1, 1990, 36)

FFF #36. A Logical "Paradox", Ed Barbeau, 22:2, 1991, 132, F (also 23:3, 1992, 205)

FFF #40. Perron's Paradox, Ed Barbeau, 22:3, 1991, 221, F, 0.2 (also 23:3, 1992, 205 and 24:3, 1993, 231)

Programs for a Logic Course, Richard F. Maruszewski, Jr., 22:3, 1991, 235-240

FFF. Red Hats, Ed Barbeau, 22:4, 1991, 307, F

FFF. Equal Unions, Ed Barbeau, 23:4, 1992, 304-305, F  
The Linear Transformation Associated with a Graph: Student Research Project, Irl C. Bivens, 24:1, 1993, 76-78, 3.1, 4.3  
Using PROLOG in Discrete Mathematics, Antonio M. Lopez, Jr., 24:4, 1993, 357-365, 3.1, 3.4  
FFF #93. An Invalid Argument, Annie Selden and John Selden, 27:1, 1996, 43-44, F  
FFF #98. Doggedly Bisexual, Ed Catherall, 27:2, 1996, 116, F  
A New Theorem on Cardinality, Charles J. Kicey, 30:1, 1999, 66, C  
FFF. There are no contradictions, Theodore G. Ammon, 31:1, 2000, 48-49, F  
A Game-Like Activity for Learning Cantor's Theorem, Shay Gueron, 32:2, 2001, 122-125, C  
Comment on *There are no contradictions*, Calvin Jongma, 32:3, 2001, 199-200, F  
Comparing Sets of the Empty Set, Allen J. Schwenk, 33:3, 2002, 232-233, C, 9.5  
Sets of Sets: A Cognitive Obstacle, Lawrence Brenton, 34:1, 2003, 31-38, 9.4  
What Did Lincoln Really Mean?, Paul K. Stockmeyer, 35:2, 2004, 103-104  
An Elementary Resolution of the Liar Paradox, James S. Walker, 35:2, 2004, 105-111  
Mind Your  $\forall$ 's and  $\exists$ 's, Stephen M. Walk, 35:5, 2004, 362-369, 4.3  
Mathematics in *War and Peace*, Arthur Neuman, 39:3, 2008, 202, C  
Dinner Tables and Concentric Circles: A Harmony of Mathematics, Music, and Physics, Jack Douthett and Richard J. Krantz, 39:3, 2008, 203-211, 3.2, 9.10  
Dependent Probability Spaces, William F. Edwards, Ray C. Shiflett, and Harris S. Shultz, 39:3, 2008, 221-226, 7.2  
Two Applications of a Hamming Code, Andy Liu, 40:1, 2009, 2-5, 9.2, 9.3  
Flaws, Fallacies, and Flimflam: The Limits of Reason, Andrea Rothbart, 42:4, 2011, 264, F  
Is Parallelism an Equivalence Relation?, Andy Liu, 42:5, 2011, 372, C, 0.3  
Sets, Planets, and Comets, Mark Baker, Jane Beltran, Jason Buell, Brian Conrey, Tom Davis, Brianna Donaldson, Jeanne Detorre-Ozeki, Leila Dibble, Tom Freeman, Robert Hammie, Julie Montgomery, Avery Pickford, and Justine Wong, 44:4, 2013, 258-264, 7.2, 9.2  
Matroids on Groups?, Jeremy S. LeCrone and Nancy Ann Neudauer, 45:2, 2014, 121-128, 3.1, 3.2, 9.4  
Story Puzzles, Oscar Levin, 45:4, 2014, 296, C, 9.2  
Knights, Knaves, Normals, and Neutrals, Jason Rosenhouse, 45:4, 2014, 297-306, 9.2  
A Powerful Method of Non-Proof, John Beam, 48:1, 2017, 52-54, C, 9.3  
UFOs in the game SET: Looking for Airplanes and Spaceships, Jonathan Needleman and Felicia Sciortino, 48:4, 2017, 249-257, 3.2, 9.2, 9.7  
Basic Theorems in the Language of Maximal Intervals, Haryono Tandra, 49:1, 2018, 41-45, 9.5  
Can a Subset's Topology Detect Continuous Extensions?, Mike Krebs, 49:2, 2018, 138-139, C, 9.8  
Tactile Tools for Teaching: Implementing Knuth's Algorithm for Mastering Mastermind, Thomas M. Fiore, Alexander Lang, and Antonella Perucca, 49:4, 2018, 278-286, 3.2, 8.1, 9.2  
A Concise Proof of the Triangle Inequality for the Jaccard Distance, Artur Grygorian and Ionut E. Iacob, 49:5, 2018, 363-365  
The Art of Logic in an Illogical World, Eugenia Cheng, 49:5, 2019, 385-388, Reviewed by Jean Marie Linhart, 10  
Solving Knights-and-Knaves with One Equation, Francesco Ciraulo and Samuele Maschio, 51:2, 2020, 82-89, 9.2, 9.4, 9.10  
The Proportion of Comets in the Card Game SET, Dan May and Dan Swenson, 51:3, 2020, 162-172, 3.2, 4.3, 6.3, 7.2, 9.2, 9.4  
What's in the Bag?, Aaron Montgomery, 52:3, 2021, 177-184, 9.4, 9.5, 9.8  
Puzzles of Cardinality, Oscar Levin & Tyler Markkanen, 52:4, 2021, 243-25, 9.2  
Report on the 12<sup>th</sup> Annual USA Junior Mathematical Olympiad, Bela Bajnok & Evan Chen, 53:1, 2022, 13-20, 0.3, 3.2, 5.4.1, 9.2, 9.3, 9.5

- The Game of Sprouts, Gordon D. Prichett, 7:4, 1976, 21-25, 3.1
- Connect-It Games, Frank Harry and Robert W. Robinson, 15:5, 1984, 411-419, 3.1
- Pascal's Triangle, Karl J. Smith, 4:1, 1973, 1-13, 0.6, 3.2
- Fibonacci Numbers and Pineapple Phyllotaxy, Judithlynne Carson, 9:3, 1978, 132-136, 5.4.1
- Computer-Generated Knight Tours, Michael Gilpin, 13:4, 1982, 252-259, 3.1, 3.3
- Isomorphisms on Magic Squares, Ali R. Amir-Moez, 14:1, 1983, 48-51, 0.2, 9.3, 9.4
- Sequences, Series, and Pascal's Triangle, Lenny K. Jones, 14:3, 1983, 253-256, C, 5.4.2, 6.3
- Paths and Pascal Numbers, John F. Lucas, 14:4, 1983, 329-341, 3.2
- A Tiling of the Plane with Triangles, Paul T. Mielke, 14:5, 1983, 377-381, 0.3, 9.3
- Pascal's Triangle, Difference Tables and Arithmetic Sequences of Order N, Calvin Long, 15:4, 1984, 290-298, 3.2, 5.4.1, 6.3
- The Pascal Polytope: An Extension of Pascal's Triangle to N Dimensions, John F. Putz, 17:2, 1986, 144-155, 3.2, 5.4.1, 6.3
- Pascal Triangles and Combinations Where Repetitions Are Allowed, Kendell Hyde, 19:1, 1988, 60-62, C, 3.2
- Musical Notes, Angela B. Shiflet, 19:4, 1988, 345-347, C, 7.2, 3.2
- It's Magic! Multiplication Theorems for Magic Squares, Daniel Widdis and R. Bruce Richter, 20:4, 1989, 301-306, 3.2, 9.3
- A Complete Solution to the Magic Hexagram Problem, Harold Reiter and David Ritchie, 20:4, 1989, 307-316, 9.2, 9.4
- Permutation Puzzles: Student Research Project, John H. Wilson, 24:2, 1993, 163-165, 3.2
- FFF. A Centennial Tribute to Sam Loyd, Dean Clark, 23:5, 1992, 402-404, F
- A Mathematical Crossword Puzzle, James Leslie, 29:4, 1998, 295, C
- Digits in Triangular Squares, Dipendra Sengupta, 30:1, 1999, 31, C
- Modeling Mathematics With Playing Cards, Martin Gardner, 31:3, 2000, 173-177
- On Lunda-Designs and the Construction of Associated Magic Squares of Order 4p, Paulus Gerdes, 31:3, 2000, 182-188, 0.3
- Numerology Marches On, David Singmaster, Lawrence Braden, Peter Y. Woo and Brian Stewart Watts, 31:3, 2000, 236-237, C
- Some New Results on Magic Hexagrams, Martin Gardner, 31:4, 2000, 274-280, 3.2
- Analyzing Games of Information, Randall McCutcheon, 32:2, 2001, 82-90
- The Lord Over Better and Worse Births, John Fossa and Glenn Erickson, 32:3, 2001, 185-193, 9.3
- Magic Squares, Finite Planes, and Points of Inflection on Elliptic Curves, Ezra Brown, 32:4, 2001, 260-267, 5.1.3, 9.3
- Miscellanea: Clock Arithmetic, Carlton A. Lane, 32:4, 2001, 317, C
- A Visit With Six, Monte J. Zerger, 33:2, 2002, 74-87, 9.3
- A Poem: A Meeting with Sunya, V. V. Dixit, 33:2, 2002, 166-167, C
- Nine Cubits or Simple Soma, Richard K. Guy and Marc M. Paulhus, 33:3, 2002, 188-195, 9.7
- The "Origin" of Geometry, Reuben Hersh, 33:3, 2002, 207-211, 0.3, 2.1
- Alice in Numberland: An Informal Dramatic Presentation in 8 fits, Robin Wilson, 33:5, 2002, 354-377
- Lewis Carroll's Amazing Number-Guessing Game, Richard F. McCoart, 33:5, 2002, 378-383, 0.2
- A 51-star U. S. Flag, Gary Kennedy, 34:2, 2003, 170-171, C
- Linearizing Mile Run Times, Garrett I. Ash, J. Marshall Ash, and Stefan Catoiu, 35:5, 2004, 370-374, 0.1
- FFF #233. Measuring humour, Timandra Harkness and Helen Pilcher, 36:1, 2005, 50-51, F
- How to Ensure That Level Heads Prevail, Shmuel Zamir and Ruma Falk, 36:5, 2005, 396, 418, C
- Graeco-Latin Squares and a Mistaken Conjecture of Euler, Dominic Klyve and Lee Stemkoski, 37:1, 2006, 2-15, 3.2, 9.4
- A Card Trick and the Mathematics Behind It, Gabriela R. Sanchis, 37:2, 2006, 103-109, 9.5
- The Non-Attacking Queens Game, Hassan Noon and Glen Van Brummelen, 37:3, 2006, 223-227, C
- We Didn't Start Mathematics (song lyrics), Brian Beasley, 38:3, 2007, 204, 209, C
- The Number-Pad Game, Alex Fink and Richard Guy, 38:4, 2007, 260-264

- Hermit Points on a Box, Richard Hess, Charles Grinstead, Marshall Grinstead, and Deborah Bergstrand, 39:1, 2008, 12-23, 0.4, 5.7.1
- Number Place – The First Sudoku, Ed Pegg, Jr., 39:1, 2008, 33, C
- Finding All Solutions to the Magic Hexagram, Alexander Karabegov and Jason Holland, 39:2, 2008, 102-106, 3.2
- They Say Mathematics is Beautiful (poem), Kung-Ming Tiong, 39:2, 2008, 128, C
- Poem: Mathematical Slumber, Lee Ann Leung, 39:4, 2008, 298, C
- Fetching Water with Least Residues, Herb Bailey, 39:4, 2008, 304-306, C, 9.3
- You *Can* Teach an Old Magician New Tricks, John P. Bonomo, 39:5, 2008, 346-356
- Tuning with Triangles, Leon Harkleroad, 39:5, 2008, 367-373, 2.2
- FFF #286. Lines of cubes in a block, Ed Barbeau, 39:5, 2008, 383, F, 3.2
- Sam Loyd's Courier Problem with Diophantus, Pythagoras, and Martin Gardner, Owen O'Shea, 39:5, 2008, 387-391, C, 0.2, 0.7
- Two Applications of a Hamming Code, Andy Liu, 40:1, 2009, 2-5, 9.1, 9.3
- Solomon's Sea and Pi, Andrew J. Simoson, 40:1, 2009, 22-32, 0.4, 2.1
- Winning at Rock-Paper-Scissors, Derek Eyler, Zachary Shalla, Andrew Doumaux, and Tim McDevitt, 40:2, 2009, 125-128, C, 7.1, 7.2
- L-Tromino Tiling of Mutilated Chessboards, Martin Gardner, 40:3, 2009, 162-168, 9.7
- Polyomino Problems to Confuse Computers, Stewart Coffin, 40:3, 2009, 169-172, 9.7
- Puzzling Mechanisms, M. Oskar van Deventer, 40:3, 2009, 173, 180-181, 193-195, 201-203, 211
- Set of Mutually Orthogonal Sudoku Latin Squares, Ryan M. Pedersen and Timothy L. Vis, 40:3, 2009, 174-180, 9.4
- Jeeps Penetrating a Hostile Desert, Herb Bailey, 40:3, 2009, 182-188, 9.9, 9.10
- Three Poems, Caleb Emmons, 40:3, 2009, 188, 0.1
- Flipping Triangles!, Marc Zucker, 40:3, 2009, 189-193, 3.1
- n*-Card Tricks, Hang Chen and Curtis Cooper 40:3, 2009, 196-201, 3.2
- Reflections on the  $N + k$  Queens Problem, R. Douglas Chatham, 40:3, 2009, 204-210, 3.2, 4.1
- Crossword Puzzle:  $\pi_1 \cong Z \oplus Z$ , Gary Kennedy, 40:3, 2009, 212
- We shall find the Cube of the Rainbow (poem), Emily Dickinson, 40:5, 2009, 336, C
- MoonPi*, Bathsheba Grossman, 40:5, 2009, 344, C
- To Divine Proportion* (poem), Rafael Alberti, 40:5, 2009, 375, C
- Brown Sharpie: Advanced Frisbee Calculus, Courtney ??, 41:1, 2010, 16, C
- Grobner Basis Representations of Sudoku, Elizabeth Arnold, Stephen Lucas, and Laura Taalman, 41:2, 2010, 101-111, 9.4
- Sonnet (poem), Susan Colley, 41:2, 2010, 144, C
- Three Poems, Nicole Yunger Halpern, 41:3, 2010, 233-234, C
- How Bound Tetrahedron Wraps a Real Tetrahedron, Roger Berry, 41:5, 2010, 356, C, 0.3
- Poem: A Little Love Story, Bonnie Shulman, 41:5, 2010, C
- Chutes and Ladders* for the Impatient, Leslie A. Cheteyan, Stewart Hengeveld, and Michael A. Jones, 42:1, 2011, 2-8, 6.3, 7.2, 9.10
- How *Iterated Möbius* was constructed, Anne Burns, 42:1, 2011, 14, C
- Mathematical Jeopardy?, Andy Liu, 42:1, 2011, 24, C
- Boundary Conditions (poem), Ursula Whitcher, 42:1, 2011, 56, C
- Mathematics at the Movies, Martin J. Erickson, 42:3, 2011, 228, C
- Folding Polyominoes from One Level to Two, Greg N. Frederickson, 42:4, 2011, 265-274, 0.3, 9.7
- The Easiest Lights Out Games, Bruce Torrence, 42:5, 2011, 361-371, 4.1, 4.3
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- Averaging Sums of Powers of Integers, Thomas J. Pfaff, 42:5, 2011, 402-403, C, 3.2, 9.3
- Hexaflexagons, Martin Gardner, 43:1, 2012, 2-5, 0.3, 3.2, 9.4, 9.8

- The V-flex, Triangle Orientation, and Catalan Numbers in Hexaflexagons, Ionut E. Iacob, Bruce McLean, and Hua Wang, 43:1, 2012, 6-10, 0.3, 3.1, 3.2, 5.4.1, 9.8
- From Hexaflexagons to Edge Flexagons to Point Flexagons, Les Pook, 43:1, 2012, 11-14, 0.3, 3.1, 9.4, 9.8
- Cups and Downs, Ian Stewart, 43:1, 2012, 15-19, 3.2, 4.1
- Martin Gardner's Mistake, Tanya Khovanova, 43:1, 2012, 20-24, 7.2
- Mad Tea Party Cyclic Partitions, Robert Bekes, Jean Pedersen, and Bin Shao, 43:1, 2012, 25-36, 3.2, 9.3
- Triangular Numbers, Gaussian Integers, and KenKen, John J. Watkins, 43:1, 2012, 37-42, 0.1, 9.3
- Carryless Arithmetic Mod 10, David Applegate, Marc LeBrun, and N. J. A. Sloane, 43:1, 2012, 43-50, 0.1, 5.4.1, 9.4
- Bracing Regular Polygons As We Race into the Future, Greg N. Frederickson, 43:1, 2012, 51-57, 0.3
- Squaring, Cubing, and Cube Rooting, Arthur T. Benjamin, 43:1, 2012, 58-63, 0.1, 0.2
- A Platonic Sextet for Strings, Karl Schaffer, 3:1, 2012, 64-69, 0.3, 3.1
- The Play's the Thing! (crossword puzzle), Gary Kennedy and Stephen Kennedy, 43:1, 2012, 70-71, 9.2
- Magic Knight's Tours, John D. Beasley, 43:1, 2012, 72-75, 9.2
- Polyomino Dissections, Tiina Hohn and Andy Liu, 43:1, 2012, 88-94, 0.3
- 30 Years of Bulgarian Solitaire, Brian Hopkins, 43:2, 2012, 135-140, 3.2, 9.3
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- RATWYT, Aviezri S. Fraenkel, 43:2, 2012, 160-164, 3.1, 3.2
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- Multi-Peg Tower of Hanoi, Paul Isihara and Doeke Buursma, 44:2, 2013, 110-116, 3.2
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- Instant Insanity II, Tom Richmond and Aaron Young, 44:4, 2013, 265-272, 3.1, 3.2
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- Chomp in Disguise, Andrew MacLaughlin and Alex Meadows, 44:4, 2013, 284-292, 3.2
- Tetris Sudoku, Philip Riley and Laura Taalman, 44:4, 2013, 292, C, 3.2
- Boggle Logic Puzzles: Minimal Solutions, Jonathan Needleman, 44:4, 2013, 293-299, 3.1, 3.2
- Domination and Independence on a Triangular Honeycomb Chessboard, Joe DeMaio and Hong Lien Tran, 44:4, 2013, 307-314, 3.1, 3.2
- Are Stupid Dice Necessary?, Frank Bermudez, Anthony Medina, Amber Rosin, and Eren Scott, 44:4, 2013, 315-322, 3.2, 7.2, 9.3
- Challenging Magic Squares for Magicians, Arthur T. Benjamin and Ethan J. Brown, 45:2, 2014, 92-100, 9.3
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- Beyond Rubik's Cube Exhibit, reviewed by Calvin Armstrong and Susan Goldstine, 45:4, 2014, 254-257, 9.4
- The Man Who Found God's Number, David Joyner, 45:4, 2014, 258-266, 9.4
- On God's Number(s) for Rubik's Slide, Michael A. Jones, Brittany C. Shelton, and Miriam E. Weaverdyck, 45:4, 2014, 267-275, 3.1, 3.2, 9.4
- Math Frenzy Crossword Puzzle, Charlie Smith, 45:4, 2014, 276-277, C
- Graph Theory Problems from Hexagonal and Traditional Chess, Stan Wagon, 45:4, 2014, 278-287, 3.1
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- Chutes and Ladders with Large Spinners, Darcie Connors and Darren Glass, 45:4, 2014, 289-295, 3.2, 7.2

- Story Puzzles, Oscar Levin, 45:4, 2014, 296, C, 9.1  
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A Prehistory of Nim, Lisa Rougetet, 45:5, 2014, 358-363, 2.2, 3.2  
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How to Win at (One-Round) War, Richard E. Chatwin and Dana MacKenzie, 46:4, 2015, 242-253, 3.2, 4.1, 9.5, 9.9  
MAA 100<sup>th</sup> Anniversary CMJ Puzzle A, David Nacin, 46:4, 2015, 254, C  
Candy Crush Combinatorics, Dana Rowland, 46:4, 2015, 255-262, 3.2  
MAA 100<sup>th</sup> Anniversary CMJ Puzzle C, David Nacin, 46:4, 2015, 263, C  
Square-Sum Pair Partitions, Gordon Hamilton, Kiran S. Kedlaya, and Henri Picciotto, 46:4, 2015, 264-269, 0.1, 9.3  
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The Settlers of Catan: Using Settlement Placement Strategies in the Probability Classroom, Jathan Austin and Susanna Molitoris-Miller, 46:4, 2015, 275-282, 7.2  
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A Magic Trick Leads to an Identity: Some Induction Fun, Robert W. Vallin, 46:4, 2015, 295-298, C, 0.9, 3.2  
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Abbott-and-Costello Numbers, Howard Sporn, 47:2, 2016, 126-132, 4.1, 9.3  
Phillip Larkin's Koan, Paisley Rekdal, 47:2, 2016, 133, C  
Proof Without Words: Matchstick Triangles, Tom Edgar, 47:3, 2016, 207, C, 9.3  
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Rankings Over Time, Michael A. Jones, Alexander Webb, and Jennifer Wilson, 47:4, 2016, 242-248, 5.4.2, 9.8  
MAA 101<sup>st</sup> Anniversary CMJ Puzzle A, David Nacin, 47:4, 2016, 249, C  
Statistics on the Bonus Round of Wheel of Fortune, Kathleen Ryan and Brittany Shelton, 47:4, 2016, 250-253, 7.3  
MAA 101<sup>st</sup> Anniversary CMJ Puzzle C, David Nacin, 47:4, 2016, 254, C  
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The FA Cup Draw and Pairing Up Probabilities, Patrick Sullivan, 47:4, 2016, 282-292, 3.2, 7.2  
MAA 101<sup>st</sup> Anniversary CMJ Puzzles Solutions, David Nacin, 47:4, 2016, 293, C  
Form (poem), Sarah Blake, 47:5, 2016, 333, C, 9.8  
Do the Twist! (on Polygon-Base Boxes), sarah-marie belcastro and Tamara Veenstra, 47:5, 2016, 340-345, 0.3, 0.6  
The Bizarre World of Nontransitive Dice: Games for Two or More Players, James Grime, 48:1, 2017, 2-9, 7.1, 7.2  
Balanced Nontransitive Dice, Alex Schaefer and Jay Schweig, 48:1, 2017, 10-16, 3.3, 7.1, 7.2  
A Plane Angle Poem, Jordie Albiston, 48:1, 2017, 30, C  
Forgotten Equations (poem), Kazim Ali, 48:2, 2017, 111, C

- Water Mathematics (poem), Donald Illich, 48:3, 2017, 170, C
- Dihedoku Puzzle 1, David Nacin, 48:4, 2017, 248, C, 9.4
- UFOs in the game SET: Looking for Airplanes and Spaceships, Jonathan Needleman and Felicia Sciortino, 48:4, 2017, 249-257, 3.2, 9.1, 9.7
- Dihedoku Puzzle 2, David Nacin, 48:4, 2017, 258, C, 9.4
- Tiling Squares with Big Holes with L-triominoes, Patrick J. Costello, 48:4, 2017, 259-263, 3.2, 9.7
- Dihedoku Puzzle 3, David Nacin, 48:4, 2017, 264, C, 9.4
- Carcassonne in the Classroom, Mindy Capaldi and Tiffany Kolba, 48:4, 2017, 265-273, 7.2
- On a Complex KenKen Problem, David Nacin, 48:4, 2017, 274-282, 9.4
- Dihedoku Puzzles Solutions, David Nacin, 48:4, 2017, 283, C, 9.4
- An Introduction to Lazy Cops and Robbers on Graphs, Brendan W. Sullivan, Nikolas Townsend, and Mikayla L. Werzanski, 48:5, 2017, 322-333, 3.1
- It's Puzzling, C. Douglas Howard, 49:4, 2018, 242-249, 4.7, 7.2, 9.10
- Knightdoku Puzzle 1, David Nacin, 49:4, 2018, 250, C
- Strange Spinners and Diversity of Dice in Chutes and Ladders, Erin Frasetto, Michael Gableman, McKenzie Lamb, Tyler Shimek, and Andrea Young, 49:4, 2018, 251-260, 3.2, 4.7, 7.2, 9.10
- Knightdoku Puzzle 2, David Nacin, 49:4, 2018, 261, C
- Variations on the Binary Mind-Reading Trick, Jonathan Hoseana, 49:4, 2018, 262-268, 0.1, 9.3
- Knightdoku Puzzle 3, David Nacin, 49:4, 2018, 269, C
- Probabilities of Qwirkle Hand Values, 49:4, 2018, 270-276, 3.2, 7.2, 9.10
- Knightdoku Puzzle 4, David Nacin, 49:4, 2018, 277, C
- Tactile Tools for Teaching: Implementing Knuth's Algorithm for Mastering Mastermind, Thomas M. Fiore, Alexander Lang, and Antonella Perucca, 49:4, 2018, 278-286, 3.2, 8.1, 9.1
- Knightdoku Puzzles Solutions, David Nacin, 49:4, 2018, 287, C
- The Solution to a Hanoi-ing Little Problem, John P. Bonomo, 49:4, 2018, 288-291, 3.3, 6.3, 8.1
- A Simple Probability Paradox, Timothy McDevitt and Angela Wesneski, 49:4, 2018, 292-294, C, 7.1, 7.2
- The Probability of Winning a Racquetball Game with Deuce, Poontarika Khotmongkon, Nahahai Rerkruthairat, Sujitra Suriwong, and Kornkanok Watcharakarn, 49:5, 2018, 353-358, 7.2
- Geek Tragedy (Poem), Kenneth Mulder, 50:2, 2019, 133, C, 5.4.2
- The n-Children Problem, John Engbers and Adam Hammett, 49:4, 2019, 242-249, 7.2
- The Choking Index: An Analysis of Performance Under Pressure on the PGA Tour, William W. Miles and Sammi E. Smith, 49:4, 2019, 260-271, 7.3
- Developing an Optimal Strategy for a Maximization Dice Game, Kevin L. T. Chan and Wai-Sum Chan, 49:4, 2019, 272-279, 7.1, 7.2, 9.10
- By the Numbers, David Richeson, 49:4, 2019, 286-287, 300(sol.), C
- Greedy Queens on an Infinite Chessboard, William Paulsen, 49:4, 2019, 288-294, 5.1.1, 5.4.1
- A Two-Dimensional Perspective on Simpson's Paradox and Its Likelihood, Michael A. Jones, 49:4, 2019, 295-297, C, 0.4, 7.3, 9.10
- Coloring a 1-by-n Chessboard, Elias Abboud, Rathi Saleh, and Amal-Sharif Rassian, 49:5, 2019, 322-330, 3.2, 5.4.2
- Solving Knights-and-Knaves with One Equation, Francesco Ciraulo and Samuele Maschio, 51:2, 2020, 82-89, 9.1, 9.4, 9.10
- The Proportion of Comets in the Card Game SET, Dan May and Dan Swenson, 51:3, 2020, 162-172, 3.2, 4.3, 6.3, 7.2, 9.1, 9.4
- How to Win at Tenzi, Steve Bacinski and Timothy Pennings, 51:4, 2020, 242-253, 4.1, 7.1, 7.2, 9.9
- Converting Between Dates in the Hebrew and Roman Calendars, John Conway , Gabrielle Agus & David Slusky , 51:5, 2020, 322-329, 0.1
- Matrix Solution to Gergonne's Pile Problem, Mervlyn Moodley, 51:5, 2020, 351-357, 4.1
- When Rooks Miss: Probability Through Chess, Stephen J. Miller, Haoyu Sheng & Daniel Turek, 52:2, 2021, 82-93, 3.2, 5.1.1, 7.2, 7.3, 9.10

Distances Between Factorizations of the Chicken McNugget Monoid, Scott Chapman, Pedro Garcia-Sanchez & Christopher O'Neill, 52:3, 2021, 158-176, 3.1, 3.2, 9.4  
Puzzles of Cardinality, Oscar Levin & Tyler Markkanen, 52:4, 2021, 243-25, 9.1  
Parking Functions: Choose Your Own Adventure, Joshua Carlson, Alex Christensen, Pamela E. Harris, Zakiya Jones & Andrés Ramos Rodríguez, 52:4, 2021, 254-26, 3.2, 7.2  
Back to the Tower, John P. Bonomo, 52:4, 2021, 265-273, 3.2, 6.3  
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Exploring and Extending the Impossible Card Location Trick, Samantha Pezzimenti, Geovanni DiCicco, Aditya Kommoju, and Dhanush Rajesh, 52:5, 2021, 356-363, 9.3  
Arranging Beetles, Robert Gallant & Georg Gunther, 53:1, 2022, 3-12, 3.1, 3.2  
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### 9.3 Number theory (also see 0.1)

The Irrationality of Certain Numbers, Peter A. Lindstrom, 1:1, 1970, 30-31, 0.2  
F(1) Rejection Theorem, Howard Sarr, 1:2, 1970, 39-40  
F(1) and F(d) Rejection Theorems, William I. Miller, 2:2, 1971, 95-96  
Pythagorean Triples by Geometry, Steven L. Kleiman, 3:1, 1972, 39-41  
Anomalous Cancellation, R. P. Boas, Jr., 3:2, 1972, 21-24  
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Fermat Numbers, W. G. Leavitt, 4:3, 1973, 7-10  
Random Sieving and the Prime Number Theorem, Karl Greger, 5:1, 1974, 41-46, 5.3.2  
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On Generalized h-Base, Norman Woo, 6:3, 1975, 16-17  
Quasi-Pythagorean Triples for an Oblique Triangle, Kay Dundas, 8:3, 1977, 152-155, 0.6  
Methods of Random Number Generation, Edwin G. Landauer, 8:5, 1977, 296-303  
A Note on Angle Construction, Richard L. Francis, 9:2, 1978, 73-75  
The Pigeonhole Principle, Kenneth R. Rebman, 10:1, 1979, 3-13, 3.1  
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Two Distinguished Integers, Ross Honsberger, 10:3, 1979, 195-197  
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The Use of Generating Functions to Discover and Prove Partition Identities, Henry L. Alder, 10:5, 1979, 318-329  
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A Combinatorial Proof of Euler's Formula, Iain T. Adamson, 11:4, 1980, 272-273, C, 3.2  
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An Elementary Gem Concerning  $\pi(n)$ , the Number of Primes less than or equal to n, Ross Honsberger, 11:5, 1980, 305-312  
Factoring Factorials, Richard J. Friedlander, 12:1, 1981, 12-20  
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Short Stories in Number Theory, Ross Honsberger, 12:1, 1981, 34-40  
Some Conjectures on Fermat's Last Conjecture, Lawrence Sher and David Sher, 12:1, 1981, 51-52, C  
Applying Complex Arithmetic, Herbert L. Holden, 12:3, 1981, 190-194, 0.6, 5.3.1, 9.5  
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- A Classroom Approach to  $x^2 + y^2 + z^2 = w^2$ , Norman Schaumberger, 12:5, 1981, 331-332, C, 0.4
- Synthetic Division Shortened, Warren Page and Leo Chosid, 12:5, 1981, 334-336, C, 0.7
- Smith Numbers, A. Wilansky, 13:1, 1982, 21, 0.1
- Semi-Regular Lattice Polygons, Ross Honsberger, 13:1, 1982, 36-44, 3.1
- A Simple Divisibility Algorithm, David Y. Hsu, 13:1, 1982, 58-59, C, 0.2
- Remark on an Elementary Gem Concerning PI(n), Branislav Martic, 13:2, 1982, 158-159, C
- Sums of Powers of the First n Integers, David Y. Hsu, 13:3, 1982, 196-197, C
- Representable Integers, Ross Honsberger, 13:4, 1982, 260-265
- Isomorphisms on Magic Squares, Ali R. Amir-Moez, 14:1, 1983, 48-51, 0.2, 5.4.1, 9.2, 9.4
- A Prime-Generating Function, Donald D. Elliot, 14:1, 1983, 57, C
- The Alluring Lore of Cyclic Numbers, Michael W. Ecker, 14:2, 1983, 105-109
- License Numbers and Divisibility Rules, Harry Hutchins, 14:2, 1983, 122-125
- Minimization Based on the Greatest Common Divisor, David Y. Hsu, 14:2, 1983, 165-166, C
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- SSD Persistence: A Mathematical System for Student Investigation, John Scheding, 14:4, 1983, 309-312, 1.2
- A Tiling of the Plane with Triangles, Paul T. Mielke, 14:5, 1983, 377-381, 0.3, 9.2
- The Address Problem, Michael Tennor, 14:5, 1983, 407-414, 0.2
- Digital Roots of Mersenne Primes and Even Perfect Numbers, Syed Asadulla, 15:1, 1984, 53-54, C
- Integer-Sided Triangles with One Angle Twice Another, R. S. Luthar, 15:1, 1984, 55-56, C, 0.6
- The Distribution of First Digits, Stephen H. Friedberg, 15:2, 1984, 120-125, 7.2
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- Pythagorean Systems of Numbers, Joseph Wiener, 15:4, 1984, 324-326, C, 0.2, 0.4
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- Generalized Pythagorean Triples, W. J. Hildebrand, 16:1, 1985, 48-52, 0.6, 5.5
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- The House Number Problem and its Variations, Joey Paul, 16:2, 1985, 108-117
- A New Divisibility Algorithm, Joseph Whittaker, 16:4, 1985, 268-276, 0.2
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- Sweeping Gestures: A Control Theory Model for Curling, Jeffrey Lawson and Matthew Rave, 51:2, 2020, 132-140, 0.4, 6.2
- The Dynamics of the Greenhouse Effect, Claire Kiers, 51:3, 2020, 182-194, 6.3
- Fold-over Regions in Nonlinear First Order PDEs, Milton F. Maritz and Marèt Cloete, 51:3, 2020, 204-215, 6.4, 6.6, 9.9
- Flattening the Curve, Gary Kennedy, 51:4, 2020, 254-259, 4.1
- Some Probability Calculations Concerning the Egyptian Game Senet, Joaquim Noqueira, Fatima Rodrigues, and Luis Trabucho, 51:4, 2020, 271-283, 5.2.6, 7.2
- A Tour of Discrete Probability Guided by a Problem in Genomics, Leonid Hanin, 51:4, 2020, 284-294, 3.2, 7.2
- Analyzing Proportionality Coefficients in Differential Equation Models*, Paul Laumakis, 51:5, 2020, 360-368, 6.1
- The Natural Frequency: More Natural and More Frequent than Expected, William R. Green, 51:5, 2020, 372-374, C, 6.2
- Two Friends and a Bike, Phillip H. Schmidt, 52:1, 2021, 11-21, 5.1.4, 9.5
- Truck Versus Human 2.0: Mathematical Follow-Up Under Increasing Pressure, and How Kepler's Laws Come to the Rescue, Miguel A. Lerma, 52:1, 2021, 22-30, 5.1.3, 6.1
- When Rooks Miss: Probability Through Chess, Stephen J. Miller, Haoyu Sheng & Daniel Turek, 52:2, 2021, 82-93, 3.2, 5.1.1, 7.2, 7.3, 9.2
- Classroom and Computational Investigations of Camel Up, Thomas J. Clark, 52:4, 2021, 289-296, 7.1, 7.2, 9.2
- Haste Makes Waste: An Optimization Problem, William Q. Erikson, 53:2, 2022, 122-133, 5.1.4, 5.1.5, 5.2.1, 5.2.2
- A New Derivation of Snell's Law Without Calculus, John A. Quintanilla, 53:2, 2022, 140-145, 0.5, 5.1.4
- Are We Ever Our Best Possible Selves? An Application of Bezout's Identity to Find Coincident Peaks of Multiple Sine Curves, James Blackburn-Lynch, 53:3, 2022, 183-189, 0.6, 9.3

## 9.11 Software for advanced topics

- A Mathematics Software Database, R. S. Cunningham and David A. Smith, 17:3, 1986, 255-266, 0.10, 3.4, 4.8, 5.8, 6.7, 7.4
- A Mathematics Software Database Update, R. S. Cunningham and David A. Smith, 18:3, 1987, 242-247, 0.10, 3.4, 4.8, 5.8, 6.7, 7.4
- The Compleat Mathematics Software Database, R. S. Cunningham and David A. Smith, 19:3, 1988, 268-289, 0.10, 3.4, 4.8, 5.8, 6.7, 7.4
- Binary Operations, David P. Kraines and Vivian Y. Kraines and David A. Smith, 21:3, 1990, 240-241, C, 9.4
- A Model for Your Curriculum?, Douglas Campbell, 22:2, 1991, 163-166
- EXP, Version 3.02 for Windows, Jon Wilkin, 27:1, 1996, 68-73, 0.10

Scientific WorkPlace, Jerry Thornhill, 27:4, 1996, 305-311  
Standard Math Interactive, William C. Bauldry, 29:3, 1998, 237-241  
Mathematica Software Review, Steven Wilkinson, 29:4, 1998, 323-329, 5.8  
Cyclone the Implicit 3D Plotter, Jon Wilkin, 30:1, 1999, 54-59, 5.8  
SAGE: Open Source Mathematics Software System, reviewed by J. K. Denny, 44:2, 2013, 149-155, C, 4.8, 5.8, 6.7, 7.4

## 10 Book Reviews

The History of the Calculus, Carl Boyer, 1:1, 1970, 60-86, summarized by Carl Boyer  
Intermediate Algebra, Joseph Newmyer and Gus Klentes, 5:1, 1974, 60-61, reviewed by Edward B. Wright  
Elementary Linear Algebra, Paul C. Shields, 5:1, 1974, 61-62, reviewed by Frank Hacker  
Elementary Functions with Coordinate Geometry, Earl Swokowski, 5:1, 1974, 62, reviewed by Harry L. Hancock  
Basic Technical Mathematics with Calculus, Allyn J. Washington, 5:1, 1974, 62-63, reviewed by Judith Gersting  
Programmed Mathematics for Nurses, George Sackheim and Lewis Robins, 5:1, 1974, 63-64, reviewed by Allen P. Angel  
Business Mathematics—A Collegiate Approach, Nelda W. Roueche, 5:2, 1974, 55-56, reviewed by Lawrence Clar  
Algebra Programmed, R. H. Alwin and R. D. Hackworth and J. Howland, 5:2, 1974, 56-57, reviewed by Gerald M. Smith  
Mathematical Ideas, 2nd ed., Charles D. Miller and Vern E. Heeren, 5:2, 1974, 57, reviewed by Peter A. Lindstrom  
Geometry: A Guided Inquiry, G. D. Chakerian and C. D. Crabill and S. K. Stein, 5:2, 1974, 57-58, reviewed by Arthur P. Dull  
Essentials of College Algebra, 2nd ed., E. F. Beckenbach and I. Drooyer and William Wooten, 5:2, 1974, 58-59, reviewed by Olene C. Zacher  
Elementary Statistics, Robert R. Johnson, 5:2, 1974, 59, reviewed by Philip F. Reichmeider  
Basic Algebra Techniques: Concepts and Manipulations, W. Burryl McWaters and Anita McWaters and Robert L. Drennen, 5:3, 1974, 41-42, reviewed by Eugene P. Cooper  
Mathematics with Applications in the Management, Natural, and Social Sciences, Margaret L. Lial and Charles D. Miller, 5:3, 1974, 42, reviewed by H. Eugene Hall  
Applied Mathematics for Technical Programs (Trigonometry), Robert G. Moon, 5:3, 1974, 42-43, reviewed by Amogene F. DeVaney  
Integrated Algebra and Trigonometry with Analytic Geometry, 3rd ed., Robert C. Fisher and Allen D. Ziebur, 5:3, 1974, 43-44, reviewed by S. C. Tefteller  
Introduction to Probability and Statistics, 5th ed., Henry L. Alder and Edward B. Roessler, 5:3, 1974, 44-45, reviewed by Alan C. Tucker  
Mathematics and Liberal Arts, Jack C. Gill, 5:4, 1974, 31-32, reviewed by Cameron Douthitt  
Analytic Geometry with Vectors, Douglas F. Riddle, 5:4, 1974, 32, reviewed by Don Gallagher  
Linear Algebra, Paul J. Knopp, 5:4, 1974, 32-33, reviewed by Shelba Morman  
Linear Mathematics, Philip Gillett, 5:4, 1974, 34, reviewed by Peter A. Lindstrom  
Understanding Statistics, 1st ed., Arnold Naiman and Robert Rosenfeld and Gene Zirkel, 6:1, 1975, 27-28, reviewed by Ara B. Sullenberger  
Precalculus Mathematics: A Functional Approach, James Connelly and Robert Fratanglo, 6:1, 1975, 28-29, reviewed by Lawrence Gilligan  
Elementary Algebra, 1st ed., Robert G. Moon and Robert D. Davis, 6:1, 1975, 29, reviewed by Thomas L. Alexander

- Conceptions of Space, Beginning Geometries for College, William Hemmer, 6:3, 1975, 27-28, reviewed by Jean B. Smith
- Basic Mathematics for Management and Economics, Lyman C. Peck, 6:3, 1975, 28, reviewed by Cherry Mauk
- Fundamental Math—A Mixed Media Program, Units I-IV, 6:3, 1975, 28-29, reviewed by R. DeJean
- The Slide Rule, Electric Hand Calculators, and Metrification in Problem Solving, 3rd ed., George C. Beakly and H. W. Leach, 6:3, 1975, 29-30, reviewed by Terral McKellips
- Modern Mathematics: An Elementary Approach, 2nd ed., Ruric E. Wheeler, 6:4, 1975, 17-18, reviewed by Lawrence A. Trivieri
- Mathematics—A Human Endeavor, Harold R. Jacobs, 6:4, 1975, 19, reviewed by Gerald M. Smith
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- Plane Trigonometry, A New Approach, C. L. Johnson, 7:1, 1976, 24-25, reviewed by Nancy Holder
- Contemporary Mathematics, Bruce E. Meserve and Max A. Sobel, 7:1, 1976, 25-26, reviewed by James G. Troutman
- Elementary Algebra: A Worktext, Vivian Shai Groza, 7:1, 1976, 25, reviewed by Ken Seydel
- Introductory Algebra, Alphonse Gobran, 7:2, 1976, 40-41, reviewed by John P. Pace
- Developing Skills in Algebra: A Lecture Work-text, J. Louis Nanny and John L. Cable, 7:2, 1976, 41-42, reviewed by Wesley W. Tom
- Arithmetic Module Series, Thomas J. McHale and Paul T. Witzke, 7:3, 1976, 38-39, reviewed by Donald E. Brown
- Elementary Functions and Analytic Geometry, Flanders and Price, 7:3, 1976, 39-40, reviewed by Mary Ann DeVincenzo
- Carl Friedrich Gauss, A Biography, Tord Hall, 7:3, 1976, 40, reviewed by Ralph Mansfield
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- Calculus, A Practical Approach, Kenneth Kalmanson and Patricia C. Kenschaft, 8:2, 1977, 89, reviewed by Dennis M. Rodriguez
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- Mathematics Method Program, John F. LeBlanc, et al., 8:3, 1977, 166-167, reviewed by Suzanne Brown
- Differential Equations and Their Applications: An Introduction to Applied Mathematics, Martin Braun, 8:4, 1977, 231-232, reviewed by David Farnsworth
- Elementary Computer Applications in Science, Engineering, and Business, Ian Barrodale, et al., 8:4, 1977, 232-233, reviewed by Samiha Mourad
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- The Ages of Mathematics(4 volumes), Michael Moffatt and Charles Flinn and Cynthia Conwell Cook and Peter D. Cook, 9:4, 1978, 222-224, reviewed by Frank Swetz
- Understanding and Programming Computers, Samiha Mourad, 9:5, 1978, 288-289, reviewed by Mary Ann DeVincenzo
- Algebra: A Fundamental Approach, William M. Setek, 9:5, 1978, 289, reviewed by Marilyn F. Semrau
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- The Historical Roots of Elementary Mathematics, Lucas N. H. Bunt, 10:4, 1979, 288-289, reviewed by Barnabas Hughes
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- Mathematical Morsels, Ross Honsberger, 11:2, 1980, 127-128, reviewed by Leon Bankoff
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- Mind Over Math, Stanley Kogelman and Joseph Warren, 12:1, 5-61, reviewed by Henry Africk
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- Two-Year College Mathematics Readings, Warren Page, ed., 13:4, 1982, 288, reviewed by J. E. Householder
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- Random Curves, Neal Koblitz, 40:2, 2009, 142-143, reviewed by Reuben Hersh
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