

2. David C. Buchthal and Douglas E. Cameron, *Modern Abstract Algebra*, PWS Publishers, Boston, MA, 1987.
3. Robert D. Carmichael, *Introduction to the Theory of Groups of Finite Order*, Dover Publications, Mineola, NY, 1956.
4. Richard A. Dean, *Classical Abstract Algebra*, Harper & Row, New York, 1990.
5. Joseph A. Gallian, *Contemporary Abstract Algebra*, 2nd edition, D. C. Heath, Lexington, MA, 1990.
6. Neal H. McCoy and Gerald J. Janusz, *Introduction to Modern Algebra*, 4th edition, Allyn & Bacon, Boston, 1987.
7. Charles C. Pinter, *A Book of Abstract Algebra*, 2nd edition, McGraw Hill, New York, 1990.
8. Elbert A. Walker, *Introduction to Abstract Algebra*, Random House/Birkhäuser, New York, 1987.

Added in proof. A later literature search uncovered the following paper in which the result given here is noted: W. Feit, R. Lyndon, and L. Scott, A remark about permutations, *J. Combinatorial Theory (A)* 18 (1975), 234–235. The following paper explores generalizations of our result: M. Herzog and K. B. Reed, Representation of permutations as products of cycles of fixed length, *J. Austral. Math. Soc.* 22(Series A) (1976), 321–331.

A Note on the Gaussian Integral

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The elementary derivation given below for the Gaussian integral

$$I = \int_0^{\infty} e^{-x^2} dx = \frac{\sqrt{\pi}}{2}$$

uses integration in Cartesian coordinates and a dilation kind of change of variable. It is a better alternative to the usual method of reduction to polar coordinates that is found in texts on advanced calculus or probability and statistics.

Let $y = xs$, $dy = xds$, then

$$\begin{aligned} I^2 &= \int_0^{\infty} \left(\int_0^{\infty} e^{-(x^2+y^2)} dy \right) dx = \int_0^{\infty} \left(\int_0^{\infty} e^{-x^2(1+s^2)} x ds \right) dx \\ &= \int_0^{\infty} \left(\int_0^{\infty} e^{-x^2(1+s^2)} x dx \right) ds \\ &= \int_0^{\infty} \left[\frac{1}{-2(1+s^2)} e^{-x^2(1+s^2)} \right]_0^{\infty} ds = \frac{1}{2} \int_0^{\infty} \frac{ds}{(1+s^2)} \\ &= \frac{1}{2} \arctan s \Big|_0^{\infty} = \frac{\pi}{4}. \end{aligned}$$

The idea utilized in this derivation is implicit in a similar method used for establishing the functional equation: $\Gamma(a)\Gamma(b) = \Gamma(a+b)B(a,b)$ for the gamma and beta function, in the special case where $a = b = \frac{1}{2}$.