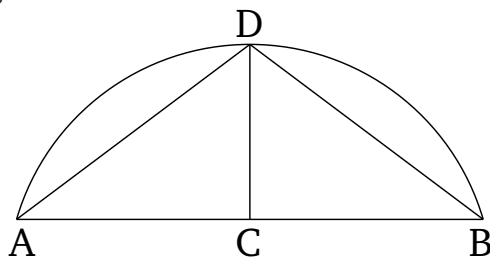


# Book 3

## Proposition 30

To cut a given circumference in half.



Let  $ADB$  be the given circumference. So it is required to cut circumference  $ADB$  in half.

Let  $AB$  have been joined, and let it have been cut in half at (point)  $C$  [Prop. 1.10]. And let  $CD$  have been drawn from point  $C$ , at right-angles to  $AB$  [Prop. 1.11]. And let  $AD$ , and  $DB$  have been joined.

And since  $AC$  is equal to  $CB$ , and  $CD$  (is) common, the two (straight-lines)  $AC$ ,  $CD$  are equal to the two (straight-lines)  $BC$ ,  $CD$  (respectively). And angle  $ACD$  (is) equal to angle  $BCD$ . For (they are) each right-angles. Thus, the base  $AD$  is equal to the base  $DB$  [Prop. 1.4]. And equal straight-lines cut off equal circumferences, the greater (circumference being equal) to the greater, and the lesser to the lesser [Prop. 1.28]. And the circumferences  $AD$  and  $DB$  are each less than a semi-circle. Thus, circumference  $AD$  (is) equal to circumference  $DB$ .

Thus, the given circumference has been cut in half at point  $D$ . (Which is) the very thing it was required to do.