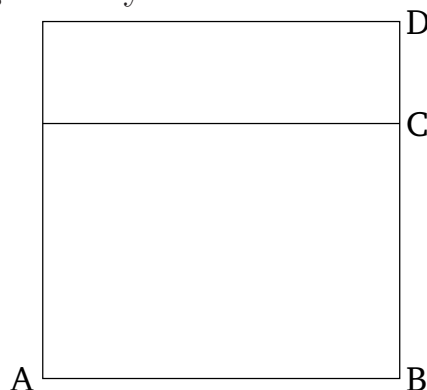


# Book 10

## Proposition 19

The rectangle contained by rational straight-lines (which are) commensurable in length is rational.

For let the rectangle  $AC$  have been enclosed by the rational straight-lines  $AB$  and  $BC$  (which are) commensurable in length. I say that  $AC$  is rational.



For let the square  $AD$  have been described on  $AB$ .  $AD$  is thus rational [Def. 10.4]. And since  $AB$  is commensurable in length with  $BC$ , and  $AB$  is equal to  $BD$ ,  $BD$  is thus commensurable in length with  $BC$ . And as  $BD$  is to  $BC$ , so  $DA$  (is) to  $AC$  [Prop. 6.1]. Thus,  $DA$  is commensurable with  $AC$  [Prop. 10.11]. And  $DA$  (is) rational. Thus,  $AC$  is also rational [Def. 10.4]. Thus, the ... by rational straight-lines ... commensurable, and so on ....