A necessary and sufficient condition is obtained for a bipartite graph to have an $f$-factor which includes a designated set of edges and is disjoint from another designated set of edges. Various other characterizations are obtained for similar subgraph structures and a characterization is obtained for a bipartite graph admitting an $f$-factor which includes no one of a collection of designated sets. (Received September 22, 2010)