



Figure 4

In Figure 4, again comparing volumes, we see that $a^2c + b^2c \geq 2abc$, and similar figures show that $a^2b + bc^2 \geq 2abc$ and $ab^2 + ac^2 \geq 2abc$.

Hence, we have $2(a^3 + b^3 + c^3) \geq 6abc$, proving Theorem 2. ■

Lemma 1 and a figure similar to Figure 2 can be used to establish the inequality $3(x^2 + y^2 + z^2) \geq (x + y + z)^2$, from which it follows that, if $d = \sqrt{x^2 + y^2 + z^2}$ is the length of the space diagonal of the rectangular box, then $d/\sqrt{3} \geq E/12$.

There are interpretations similar to (2) of the terms of Maclaurin’s inequality for $n \geq 4$ in terms of n -dimensional volumes of *hyperrectangles* (or *n-orthotopes*) and their lower-dimensional facets. We leave the details to the interested reader.

REFERENCE

1. I. Ben-Ari, K. Conrad, Maclaurin’s inequality and a generalized Bernoulli inequality, *Math. Mag.*, **87** (2014), 14–24.

Summary. We interpret the terms of Maclaurin’s inequality for three nonnegative numbers as the volume, total face area, and total side length of a rectangular box and provide a visual proof of the inequality.

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T	R	I	G		T	A	C	K	S		N	A	P		
O	P	A	L		S	A	F	A	R	I		A	R	I	
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A	C	T			T	A	U		I	S	E				
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			H	I	S		O	N	O			R	A	D	
E	F	F	O	R	T			C	H	I	C	A	G	O	
S	L	I	T			L	C	A		C	O	S	E	T	
T	A	L	I	T	H	I	A		R	E	P				
A	P	E			S	U	B	R	O	U	T	I	N	E	S
T	A	T			A	M	E	L	I	E		E	Y	R	E
E	N	S			R	E	R	I	G			D	U	S	A